



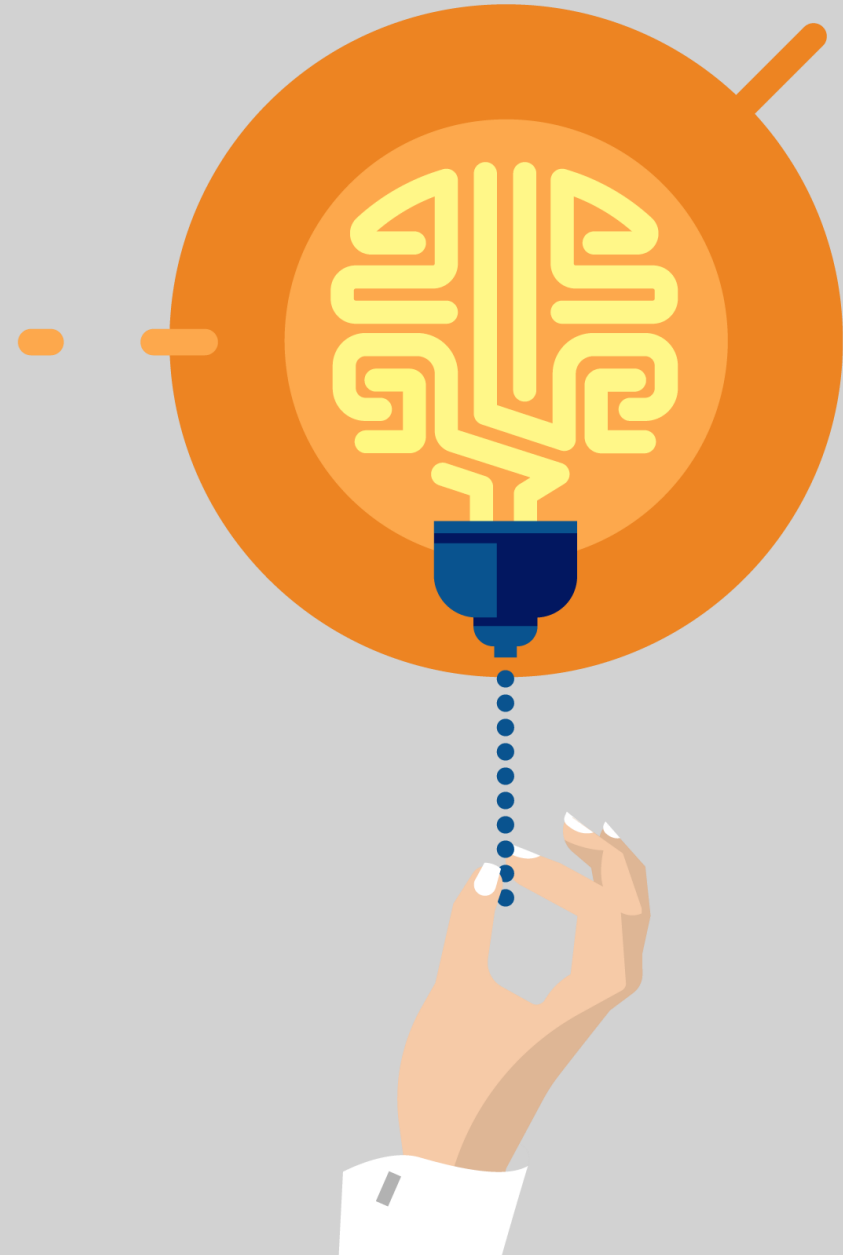
# Graph Neural Networks in Software Engineering Research

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TU Delft 2020 – IN4334



# Background



# Machine Learning



## Machine Learning Model

Designed by humans

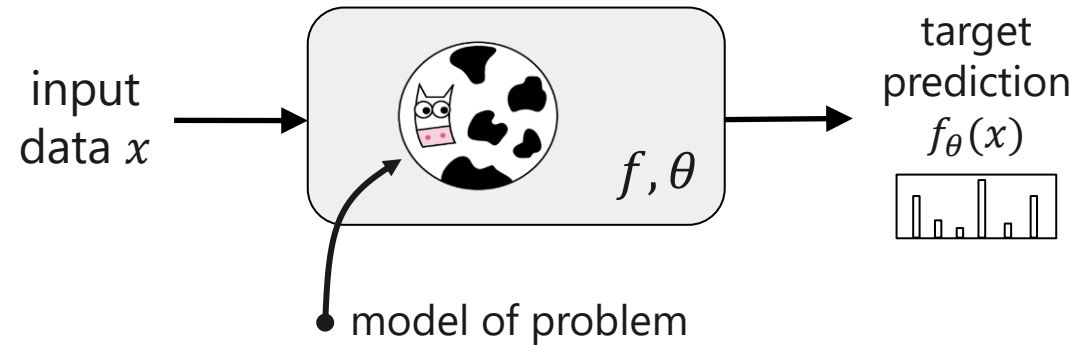


## Model Parameters

Learned from data

*"All models are wrong,  
some are useful"*  
– George Box

# Supervised Machine Learning



- Given an i.i.d. dataset  $\{(x_1, y_1), \dots, (x_N, y_N)\}$
- Pick  $\theta$  that minimize Loss  $\mathcal{L}(\theta) = \frac{1}{N} \sum_i L(f_\theta(x_i), y_i)$

# Gradient Descent: Learning Model Parameters $\theta$

while not converged

- Compute (estimate of) derivative  $g \approx \nabla_{\theta} \mathcal{L}(\theta)$
- Update  $\theta \leftarrow \theta - \eta(g)$

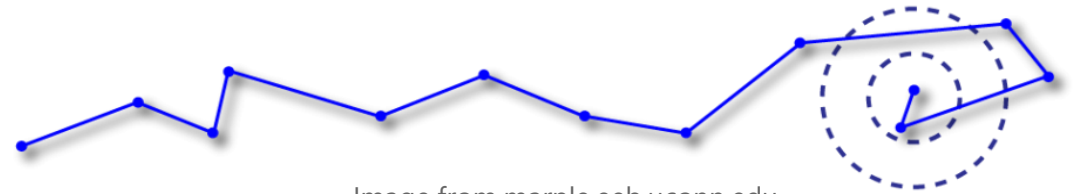


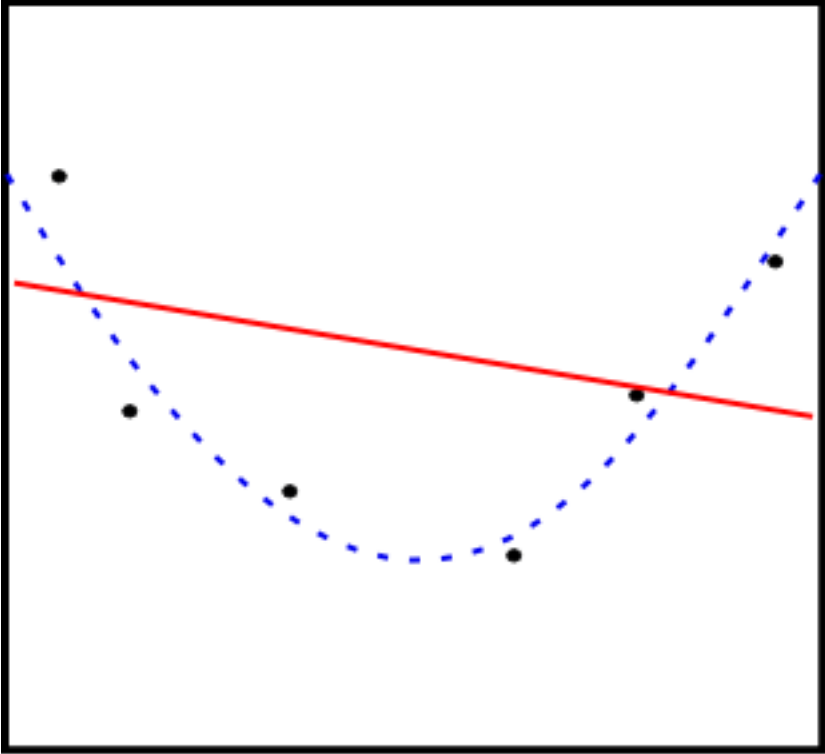
Image from marple.eeb.uconn.edu



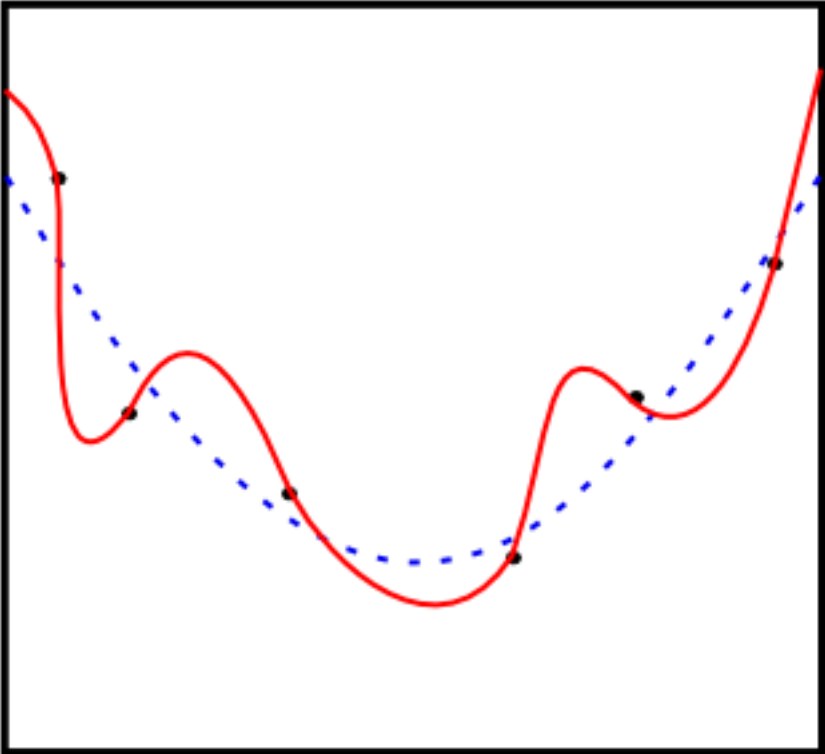
➤ Minimize loss function in training set

➤ Use computational methods of optimization

# Generalization



Underfitting

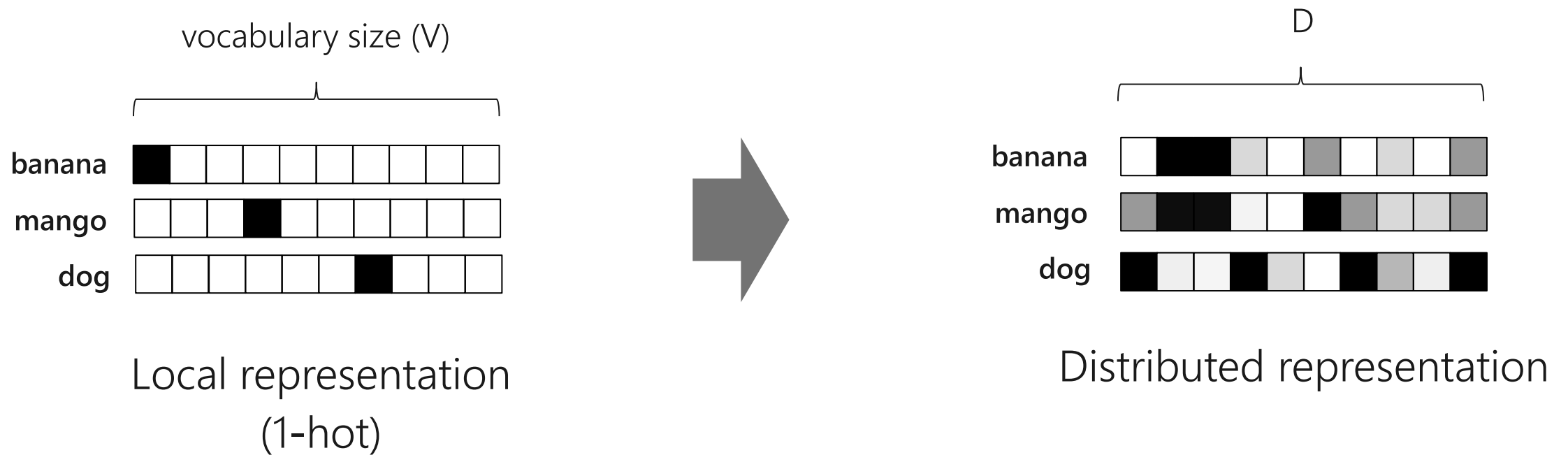


Overfitting

graphs from <http://antianti.org/?p=175>



# Distributed Vector Representations

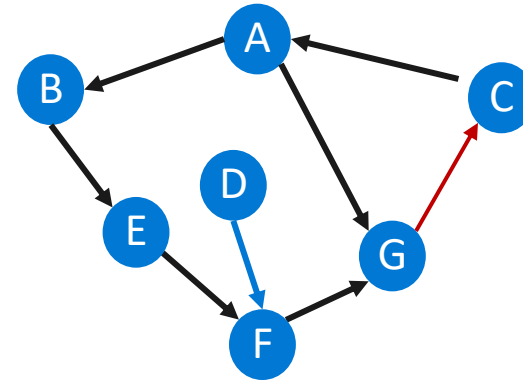


$$\mathbf{r} = E \mathbb{I}_w \text{ with } E \text{ a } D \times V \text{ matrix}$$

↑  
"vocabulary"

# Graph Notation

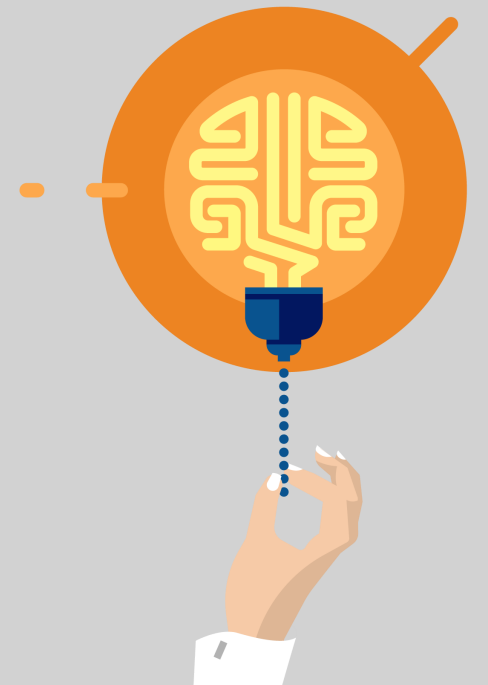
- Nodes/Vertices
- Edges/Links



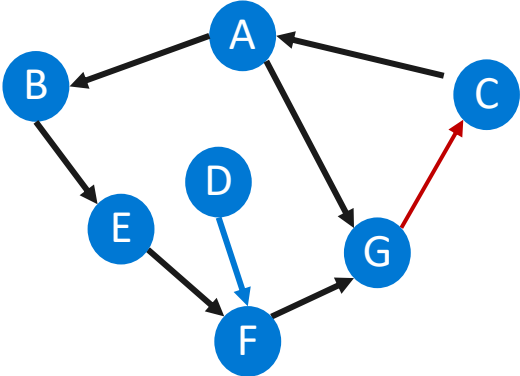
$$G = (V, E)$$

# Graph Neural Networks

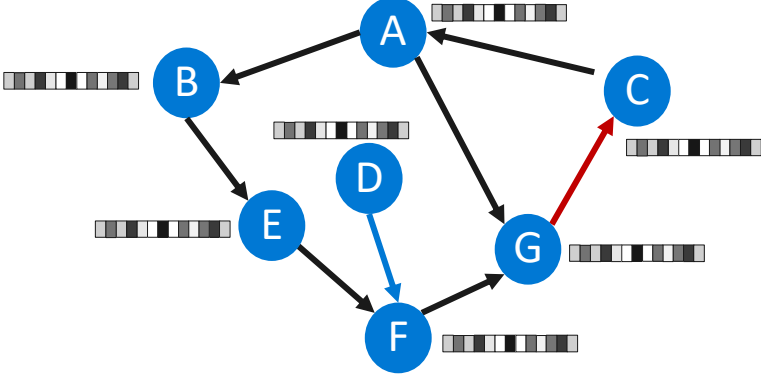
and Neural Message Passing



# Graph Neural Networks

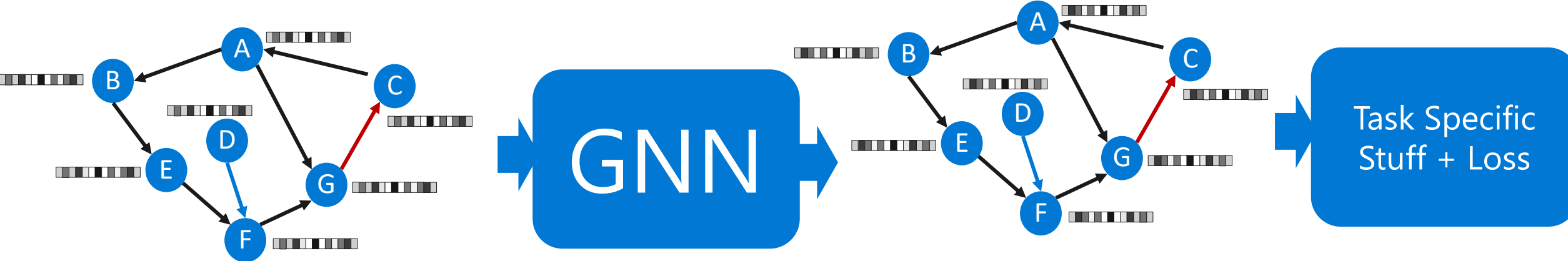


Graph Representation  
of Problem



Initial Representation  
of each node

# Graph Neural Networks

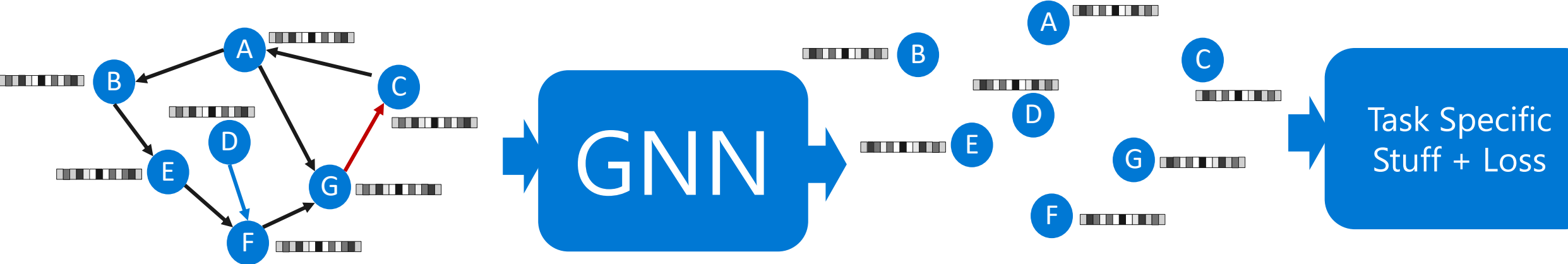


Initial Representation of each node

Output Representations of each Node

Task Specific Stuff + Loss

# Graph Neural Networks

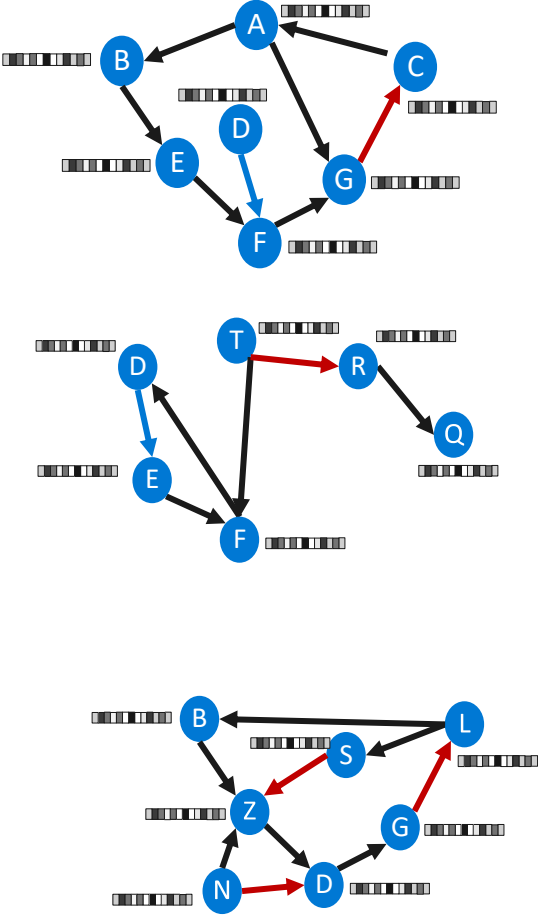
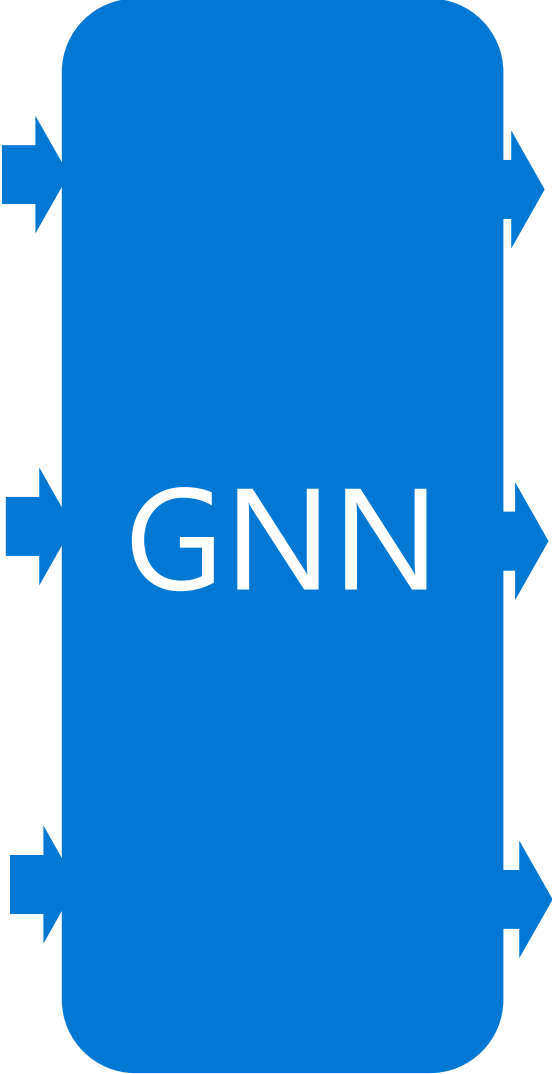
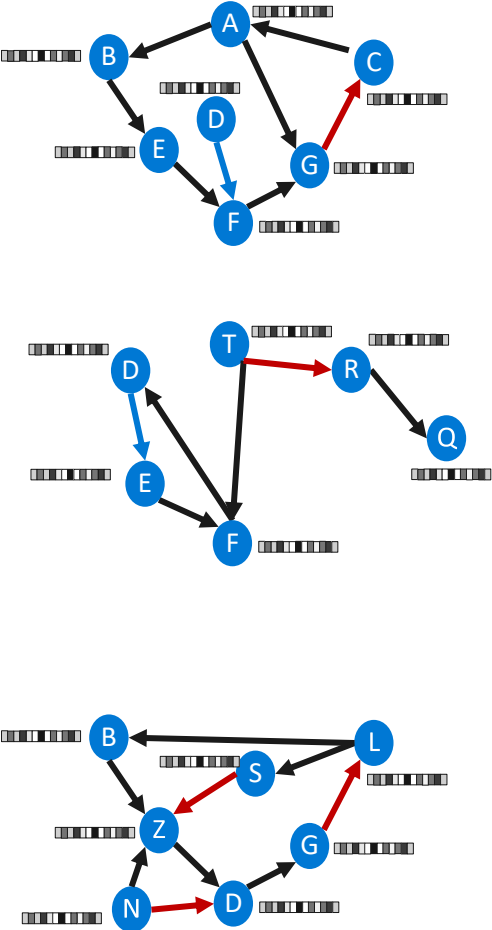


Initial Representation of each node

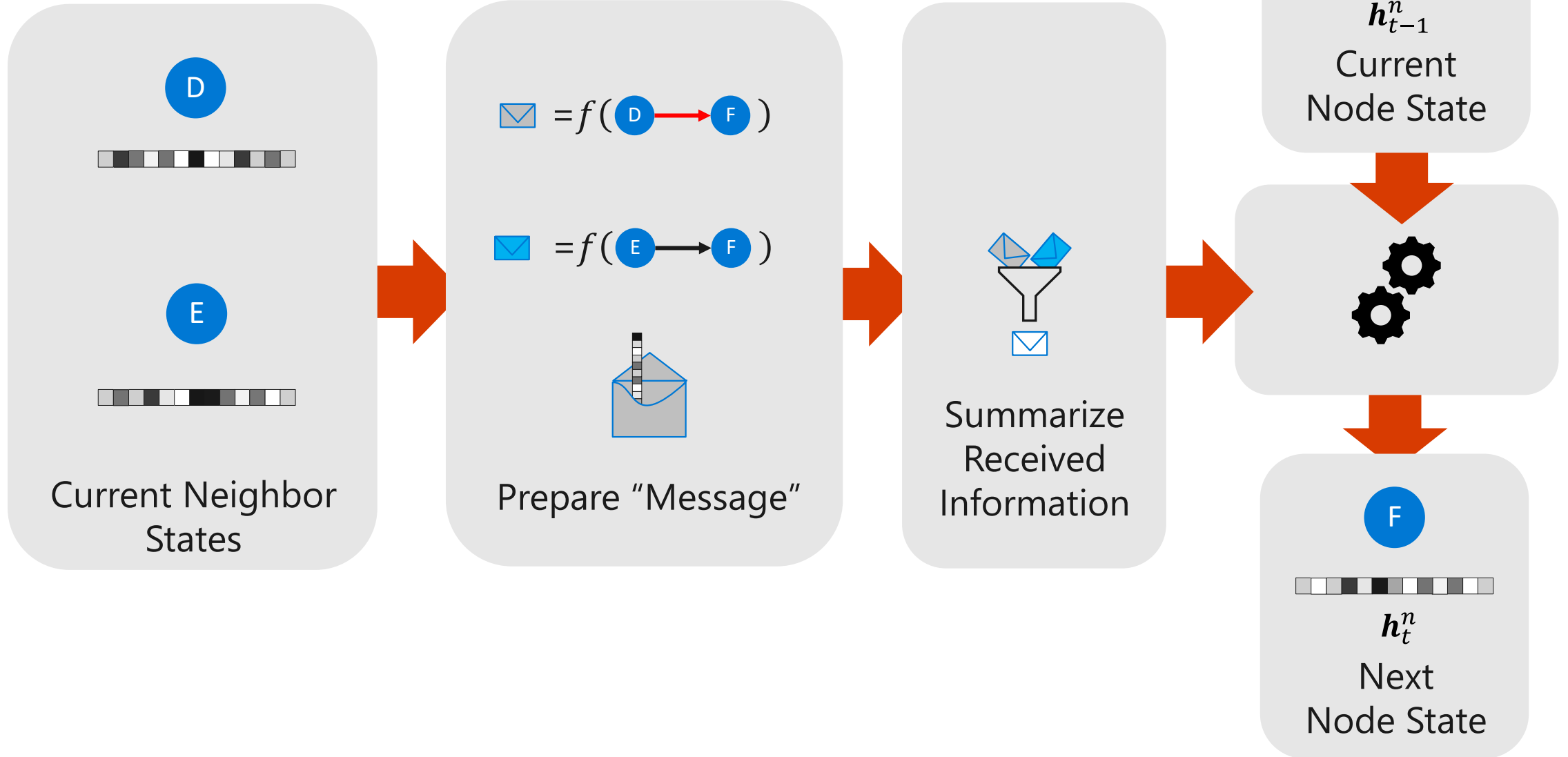
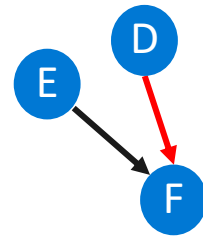
Output Representations of each Node

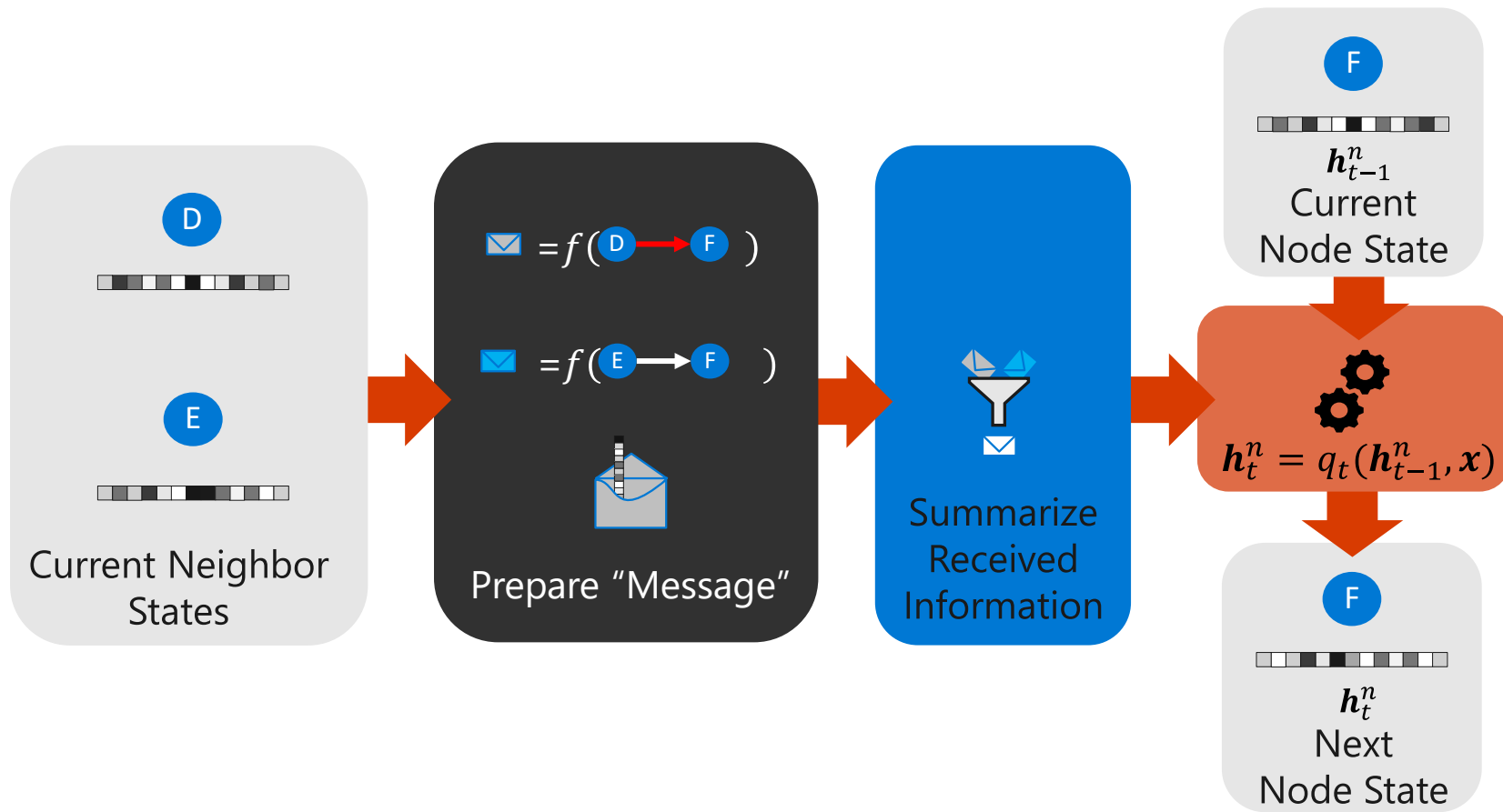
Task Specific Stuff + Loss

# Graph Neural Networks



# Neural Message Passing





$$\mathbf{h}_0^n = \mathbf{x}_n, \forall n$$

for  $t = 0 \dots T$  do

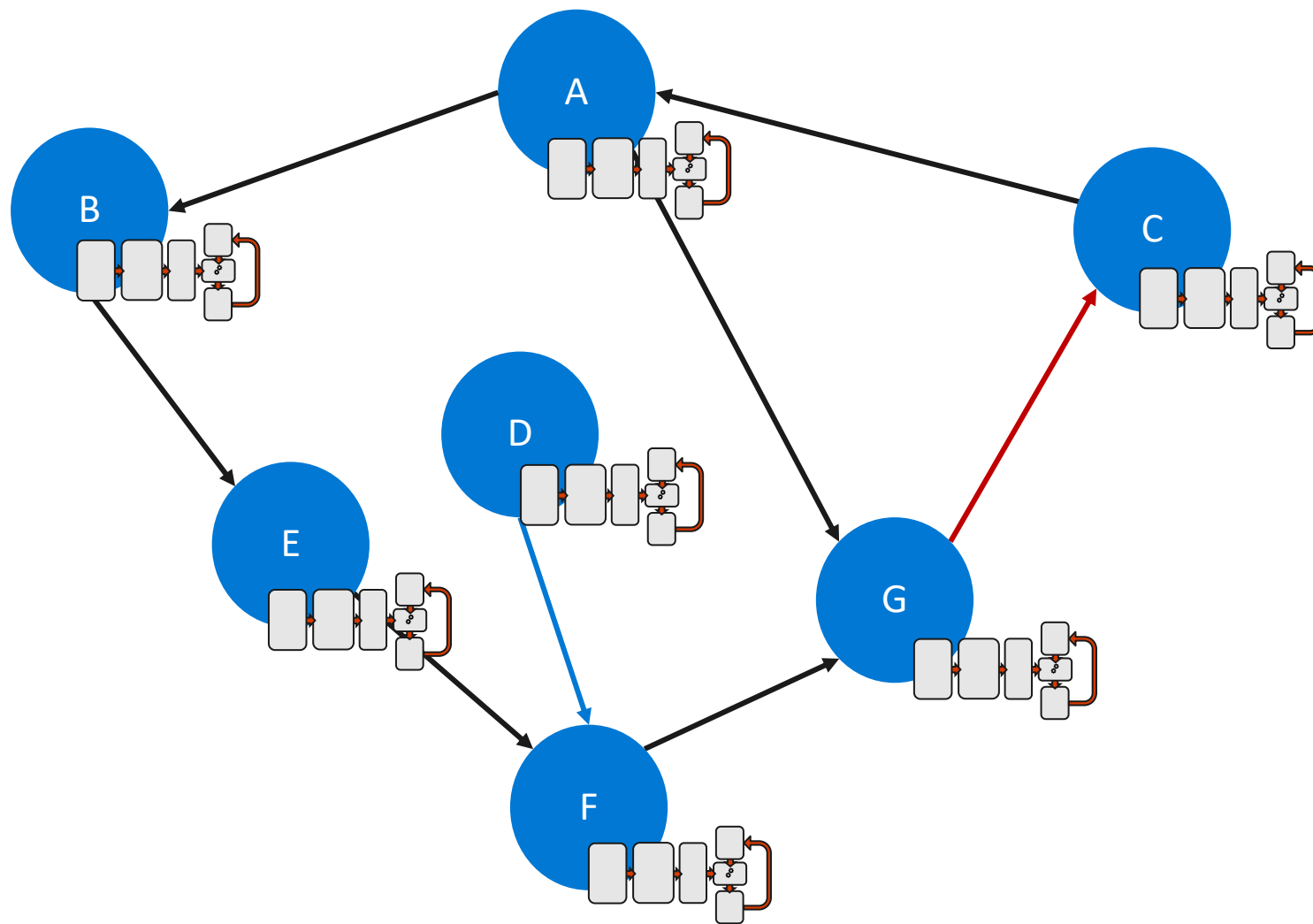
for  $n \in V$  do

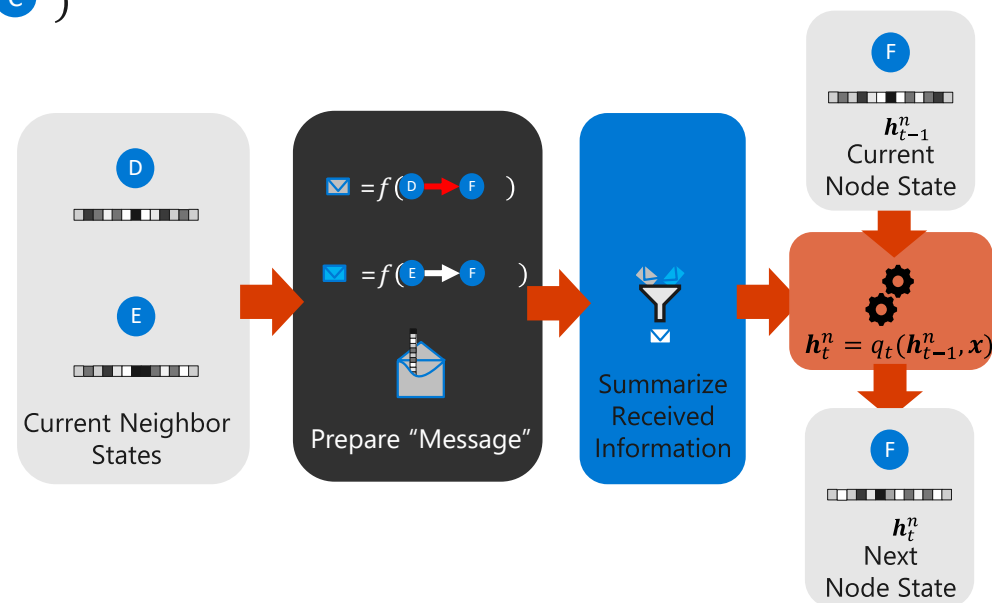
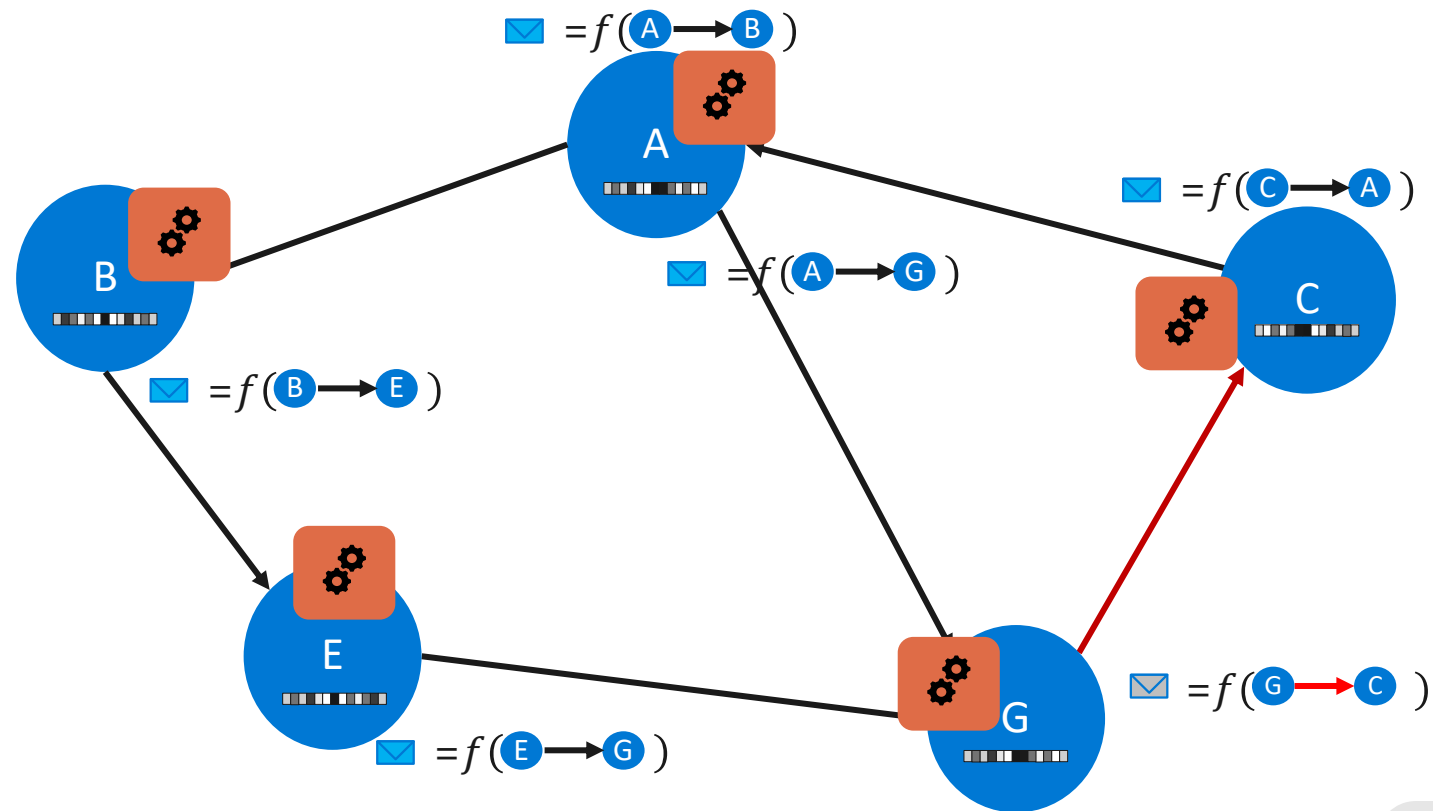
$$\mathbf{a}_t^n = \text{Aggregate}(\{\mathbf{h}_t^v | v \in \mathcal{N}(n)\})$$

$$\mathbf{h}_{t+1}^n = \text{Update}(\mathbf{a}_t^n, \mathbf{h}_{t+1}^n)$$

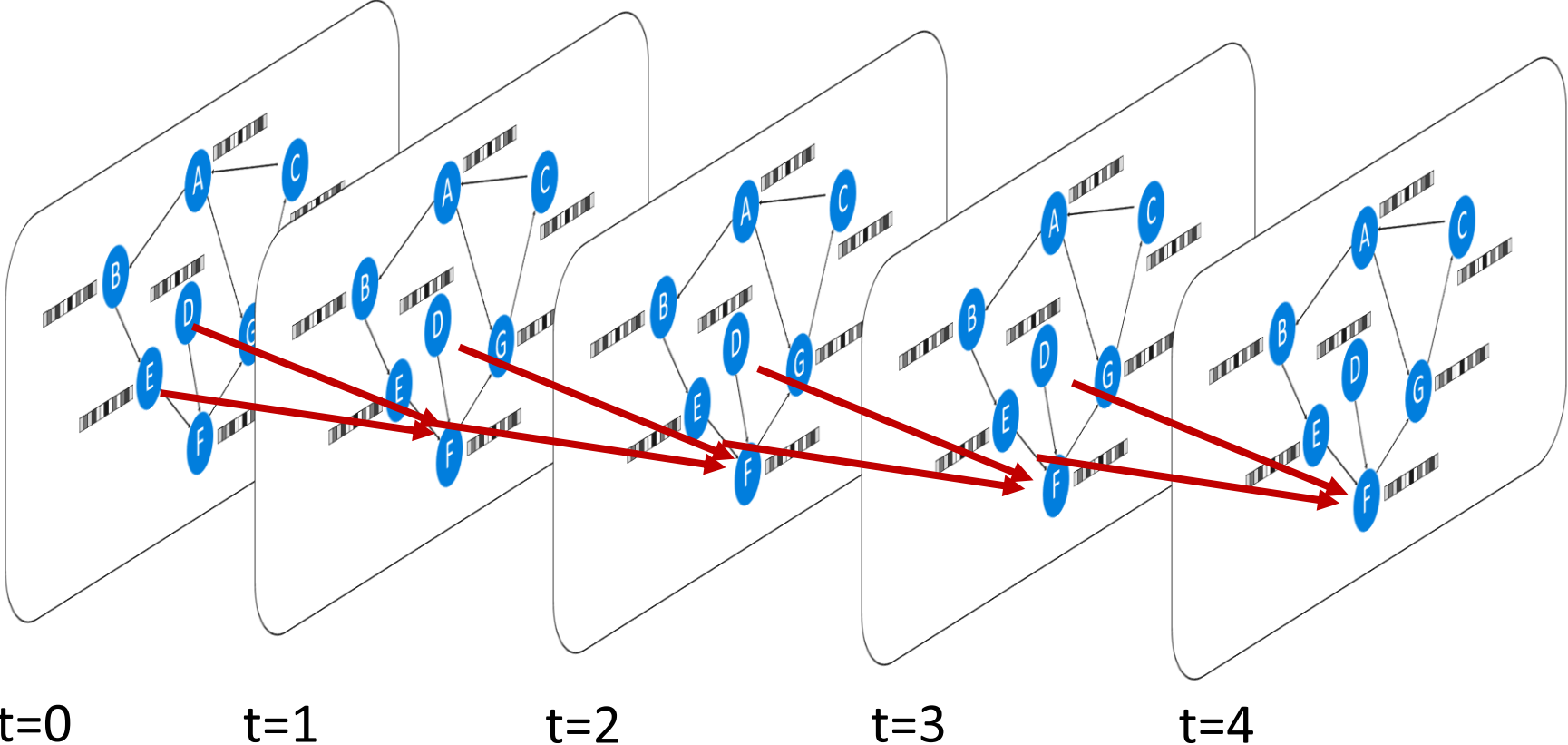
return  $\{\mathbf{h}_T^n\}$

$$\mathbf{h}_t^n = q_t \left( \mathbf{h}_{t-1}^n, \bigcup_{n_j: n_j \rightarrow n}^k f_t \left( \mathbf{h}_{t-1}^n, k, \mathbf{h}_{t-1}^{n_j} \right) \right)$$

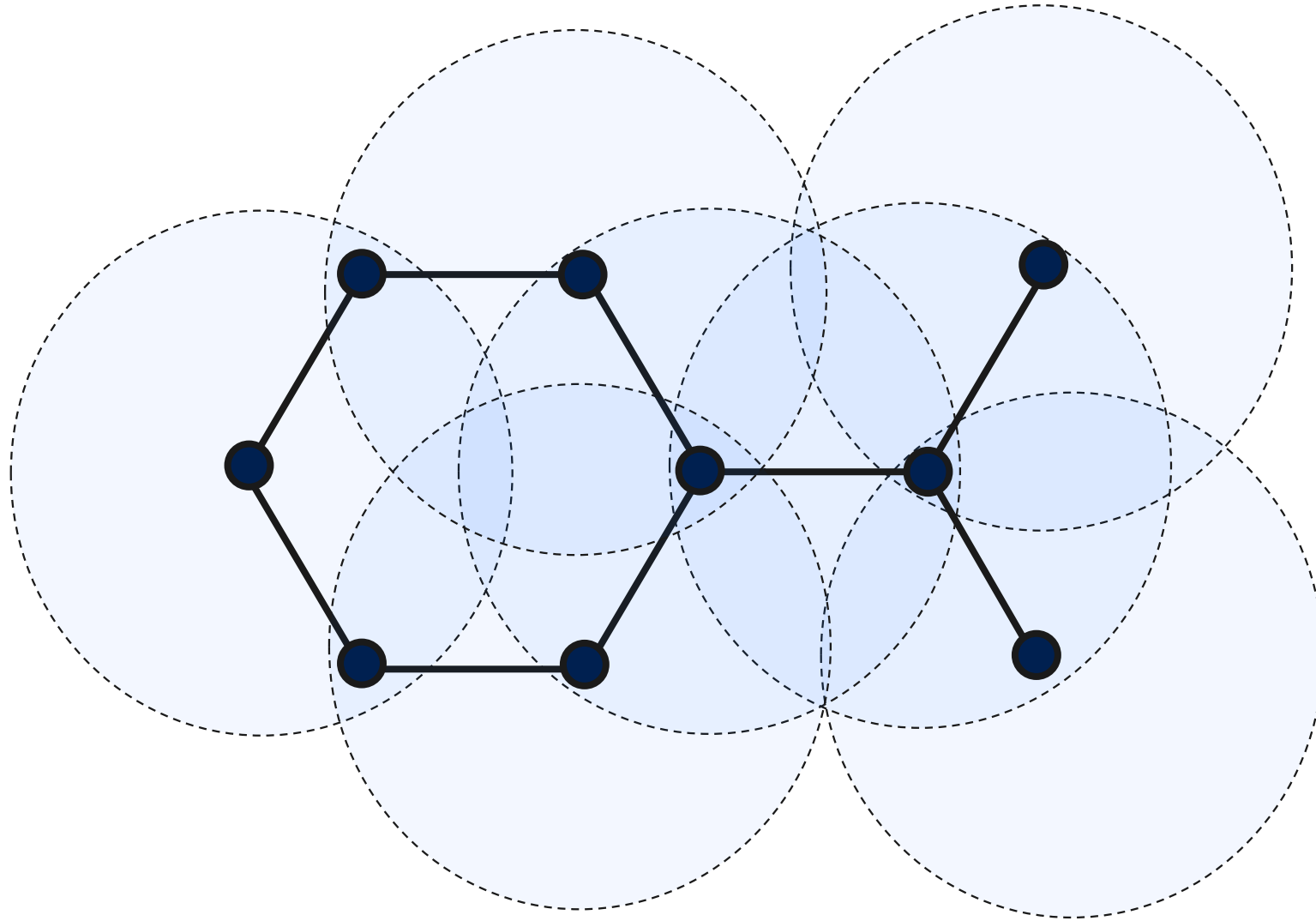




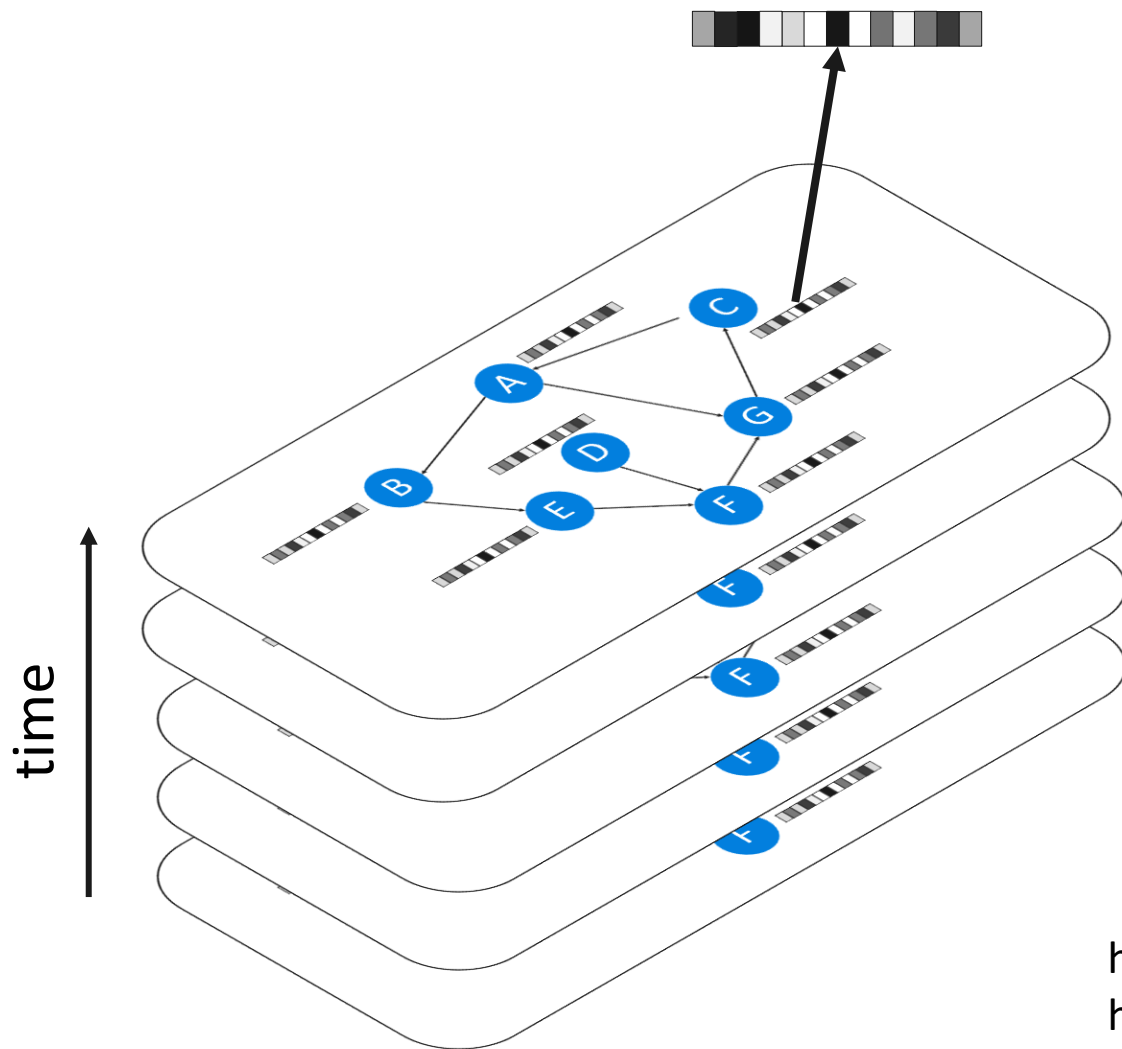
# Graph Neural Networks: Message Passing



# GNNs: Synchronous Message Passing



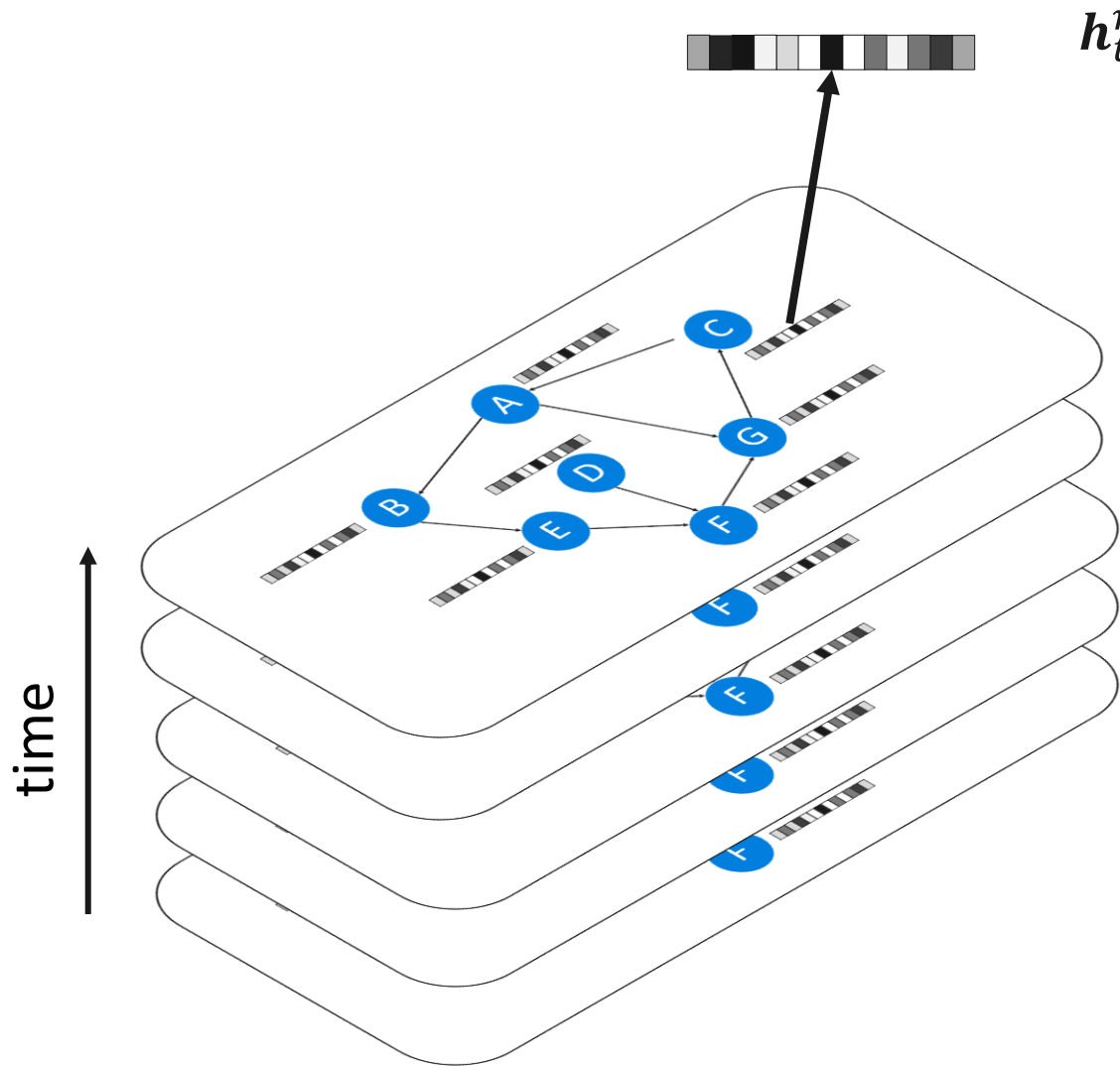
# Graph Neural Networks: Output



- node selection
- node classification
- graph classification

<https://github.com/microsoft/ptgnn/>  
<https://github.com/microsoft/tf2-gnn/>

# Example: Node [Binary] Classification

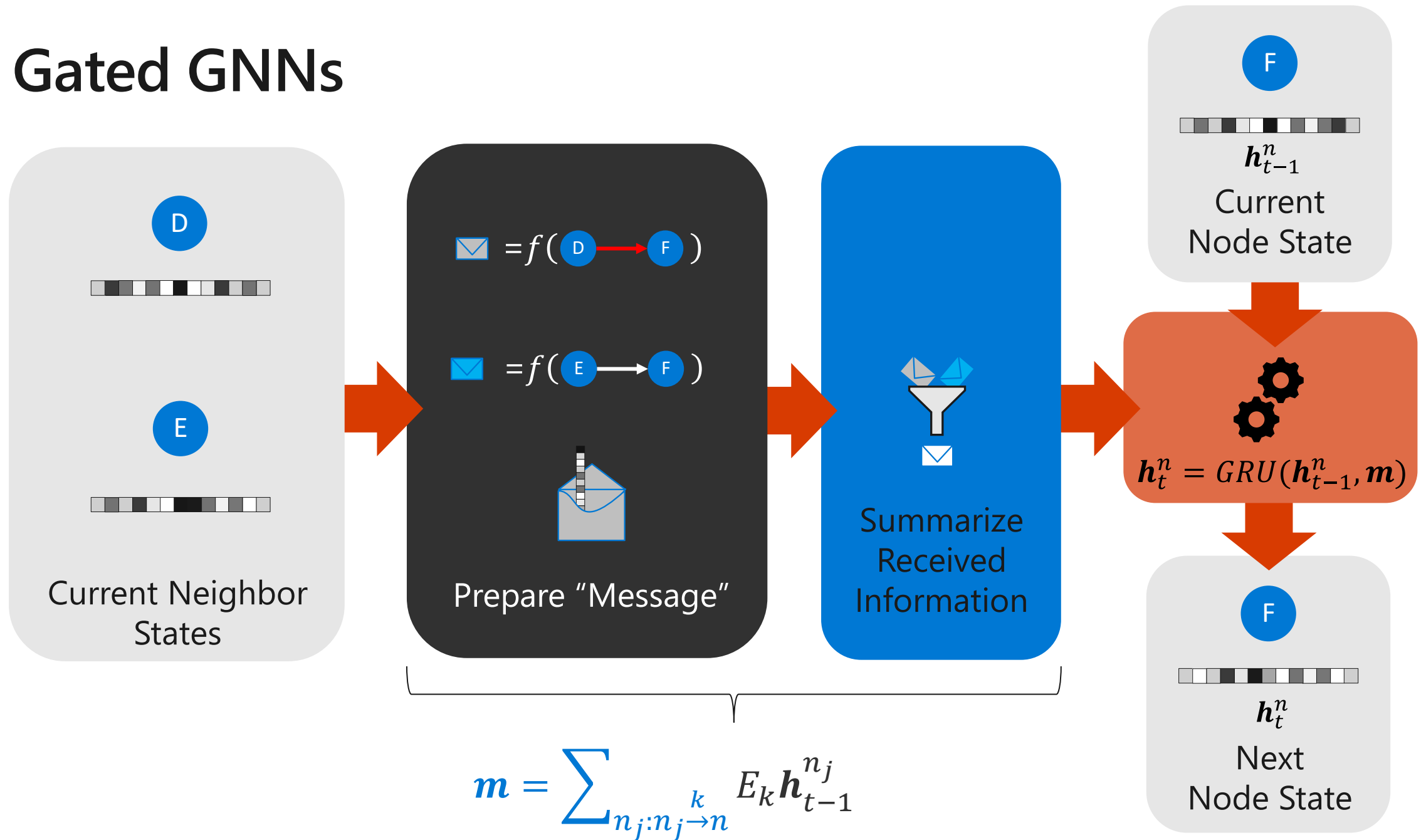


$$x_n = \sigma(\mathbf{w}^T \mathbf{h}_t^n + b)$$

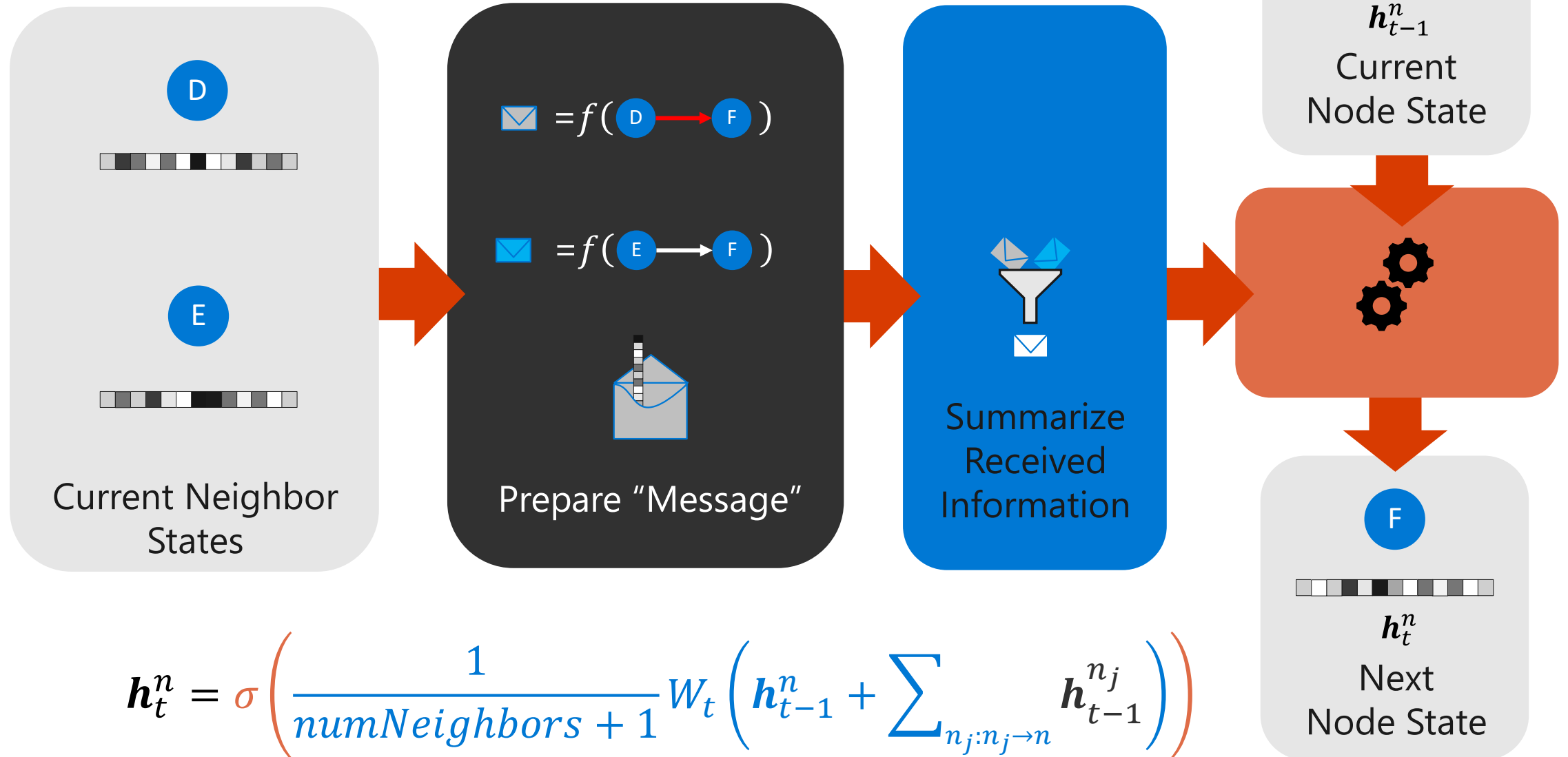
Binary cross entropy

$$\mathcal{L}(x_n, y_n) = y_n \cdot \log x_n + (1 - y_n) \log(1 - x_n)$$

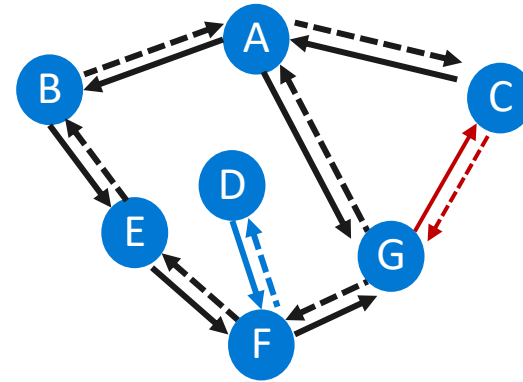
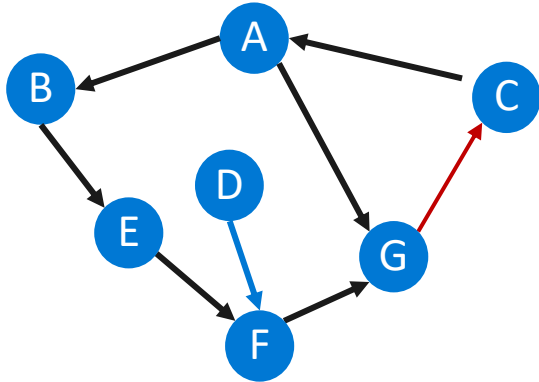
# Gated GNNs



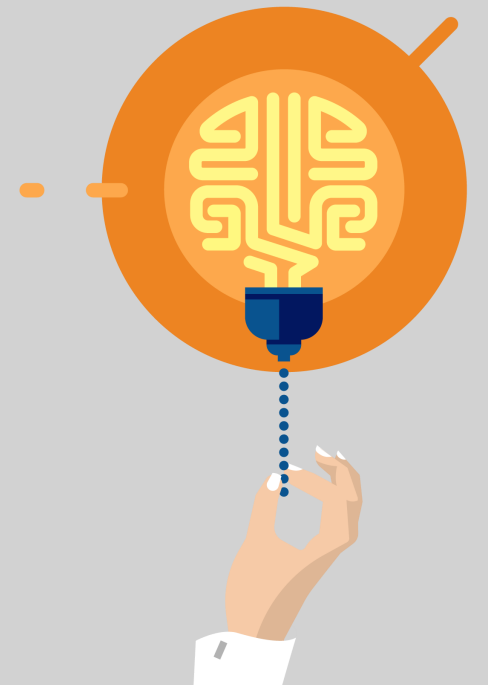
# GCNs



# Trick 1: Backwards Edges

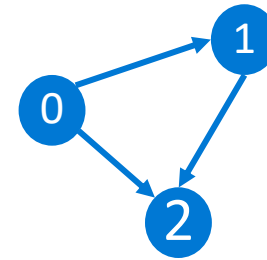


# Expressing GGNNs as Matrix Operations



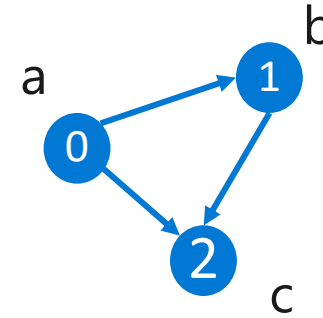
# Graph Notation (2) — Adjacency Matrices

$$A = \begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix}$$



# Graph Notation (2) — Adjacency Matrices

$$A = \begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix}, \quad N = \begin{bmatrix} a \\ b \\ c \end{bmatrix}$$

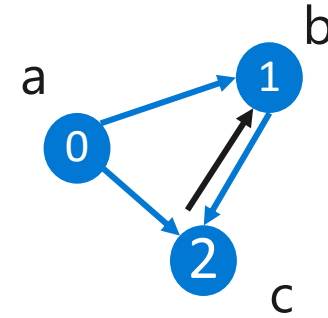


$$A \cdot N = \begin{bmatrix} 0 \\ a \\ a + b \end{bmatrix}$$

# Graph Notation (2) — Adjacency Matrices

$$A_0 = \begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix},$$

$$A_1 = \begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$



# GGNN as Matrix Operation

## Node States

$$H_t = \begin{bmatrix} \mathbf{h}_t^{n_0} \\ \vdots \\ \mathbf{h}_t^{n_K} \end{bmatrix} \quad (\text{num\_nodes} \times D)$$

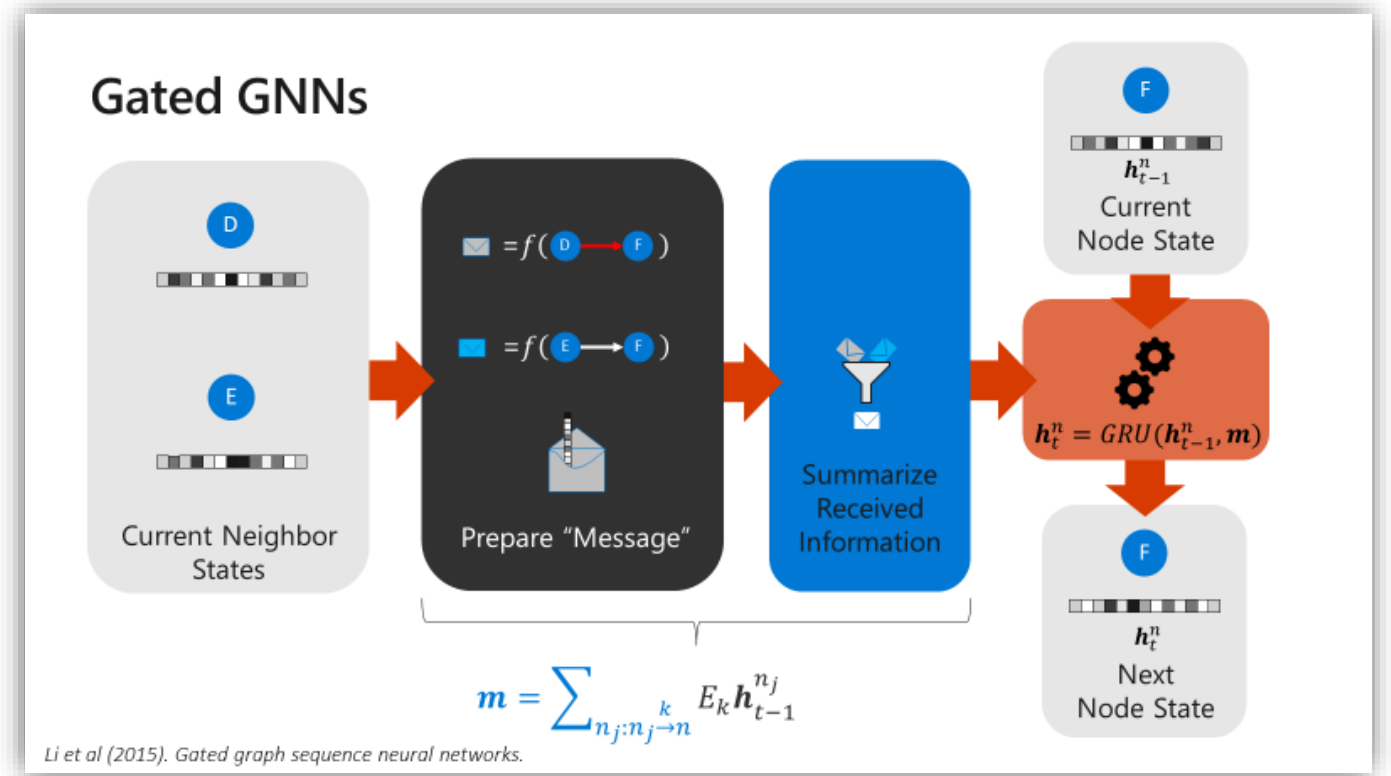
## Messages to-be sent

$$M_t^k = E_k H_t \quad (\text{num\_nodes} \times M)$$

## Received Messages

$$R_t = \sum_k A_k M_t^k \quad (\text{num\_nodes} \times M)$$

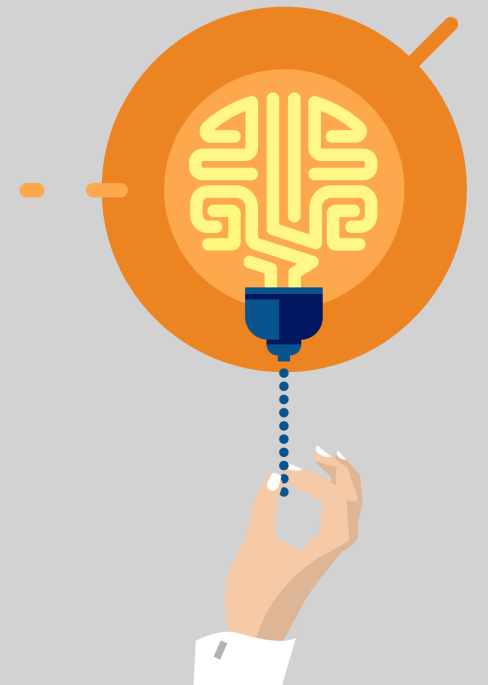
Update  $H_{t+1} = GRU(H_t, R_t)$



If we used a vanilla RNN instead

$$H_{t+1} = \sigma(UH_t + WR_t)$$

# Expressing GNN Matrix Operations as Code





# einsum

`C=np.einsum('td,qd->tq', A, B)`    #  $C_{t,q} = \sum_d A_{t,d} B_{q,d}$

`D=np.einsum('abc,be,abq->cqe', A, B,C)`

#  $D_{c,q,e} = \sum_b \sum_a A_{a,b,c} B_{b,e} C_{a,b,q}$

# GGNN as Pseudocode

```
def GGNN(initial_node_states, adj, num_steps):
    node_states = initial_node_states # [N, D]

    for i in range(num_steps):
        messages = {}
        for k in range(num_message_types):
            messages[k] = einsum('nd,dm->nm', node_states, edge_transform[k]) # [N, M]

        received_messages = zeros(num_nodes, M) # [N, M]
        for k in range(num_message_types):
            received_messages += einsum('nm,nl->lm', messages[k], adj[k])

        node_states = GRU(node_states, received_messages)

    return node_states
```

$N \times N$

# GGNN as Pseudocode

```
def GGNN(initial_node_states, adj, num_steps):
    node_states = initial_node_states # [N, D]

    for i in range(num_steps):
        messages = {}
        for k in range(num_message_types):
            messages[k] = einsum('nd,dm->nm', node_states, adj[k])

        received_messages = zeros(num_nodes, M) # [N, M]
        for k in range(num_message_types):
            received_messages += einsum('nm,nl->lm', messages[k], adj[k])

        node_states = GRU(node_states, received_messages)

    return node_states
```

## Node States

$$H_t = \begin{bmatrix} \mathbf{h}_t^{n_0} \\ \vdots \\ \mathbf{h}_t^{n_K} \end{bmatrix} \quad (\text{num\_nodes} \times D)$$

## Messages to-be sent

$$M_t^k = E_k H_t \quad (\text{num\_nodes} \times M)$$

## Received Messages

$$R_t = \sum_k A M_t^k \quad (\text{num\_nodes} \times M)$$

## Update $H_{t+1} = GRU(H_t, R_t)$

# GGNN as Pseudocode

```
def GGNN(initial_node_states, adj, num_steps):
    node_states = initial_node_states # [N, D]
```

```
    for i in range(num_steps):
```

```
        messages = {}
```

```
        for k in range(num_message_types):
```

```
            messages[k] = einsum('nd,dm->nm', node_states, edge_transform[k]) # [N, M]
```

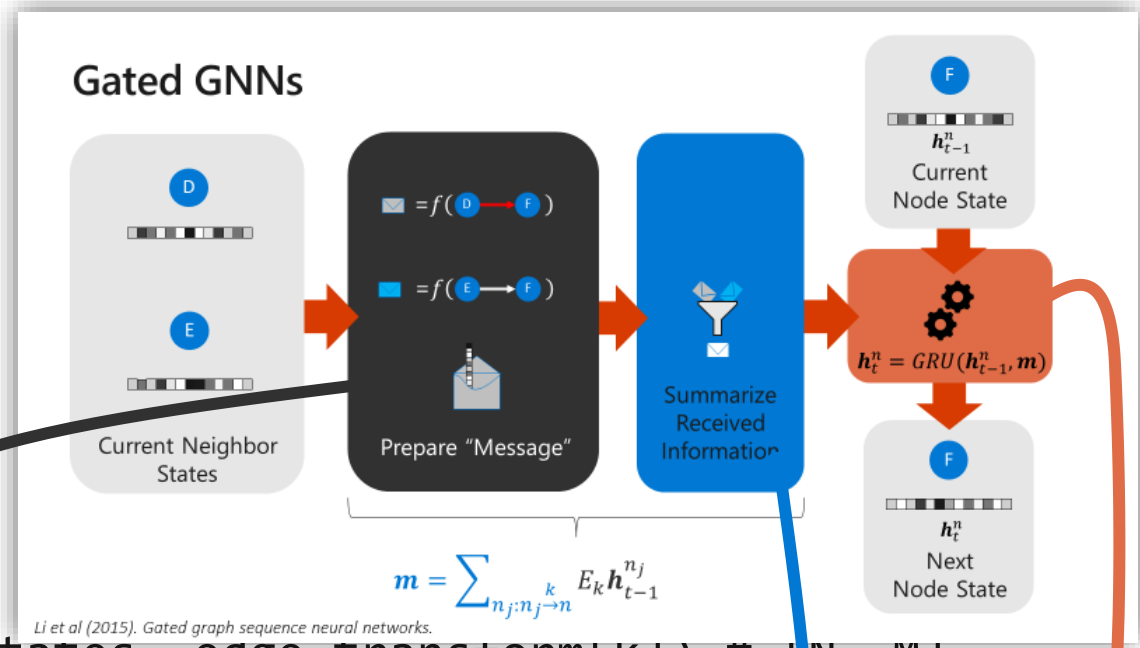
```
        received_messages = zeros(num_nodes, M) # [N, M]
```

```
        for k in range(num_message_types):
```

```
            received_messages += einsum('nm,nl->lm', messages[k], adj[k])
```

```
        node_states = GRU(node_states, received_messages)
```

```
    return node_states
```



N x N

```
def GGNN(initial_node_states, adj, num_steps):
    node_states = initial_node_states # [N, D]

    for i in range(num_steps):
        messages = {}
        for k in range(num_message_types):
            messages[k] = einsum('nd,dm->nm', node_states, edge_transform[k]) # [N, M]

        received_messages = zeros(num_nodes, M) # [N, M]
        for k in range(num_message_types):
            received_messages += einsum('nm,nl->lm', messages[k], adj[k])

        node_states = GRU(node_states, received_messages)

    return node_states
```

Find the  
parameters!

?

# GGNN as Pseudocode: Sparsity

```
def GGNN(initial_node_states, adj, num_steps):
    node_states = initial_node_states # [N, D]

    for i in range(num_steps):
        messages = {}
        for k in range(num_message_types):
            messages[k] = einsum('nd,dm->nm', node_states, edge_transform[k]) # [N, M]

        received_messages = zeros(num_nodes, M) # [N, M]
        for k in range(num_message_types):
            received_messages += einsum('nm,nl->lm', messages[k], adj[k])

        node_states = GRU(node_states, received_messages)

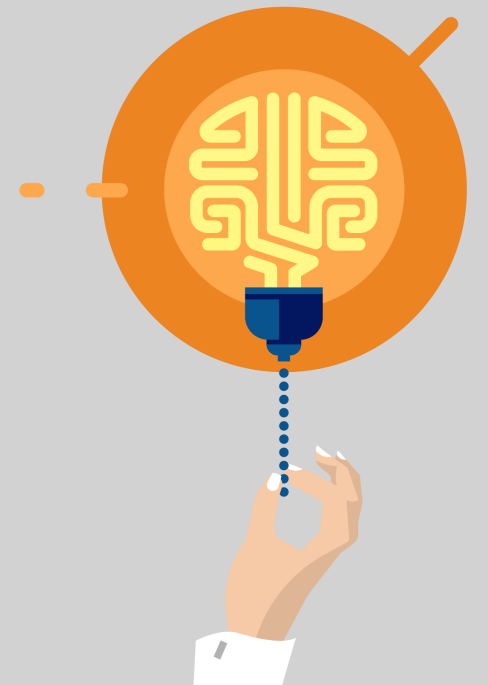
    return node_states
```

N x N



Memory

# Other Models as Special Cases of GNNs



# Special Case 1: Convolutions (CNN)

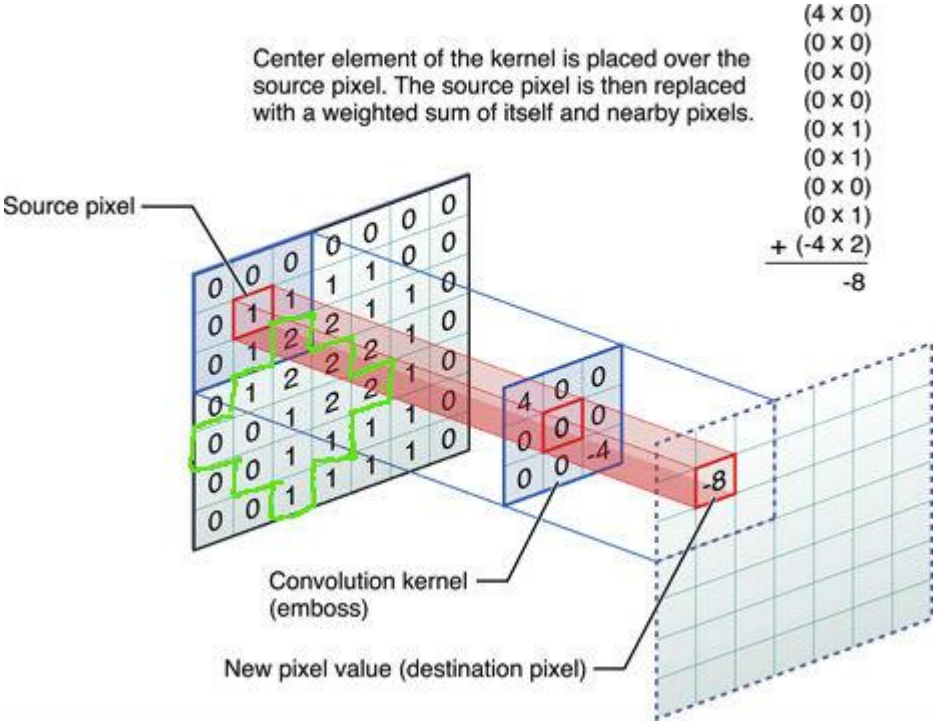
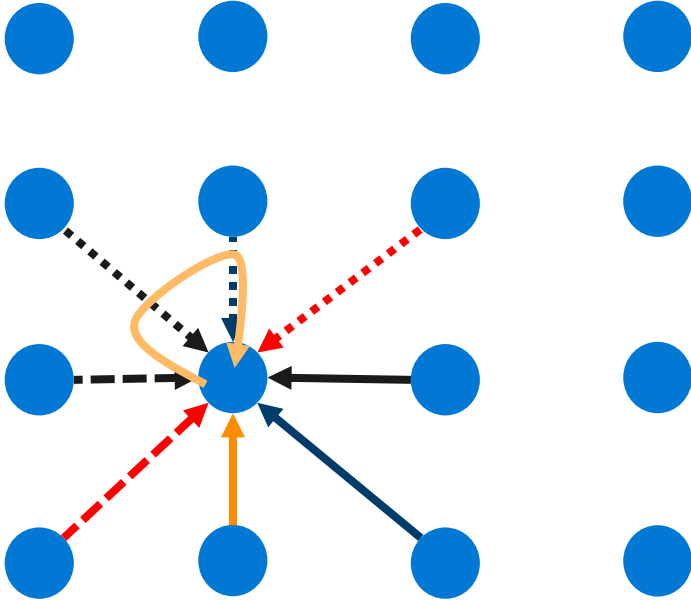


Image from: <https://stats.stackexchange.com/questions/235032>

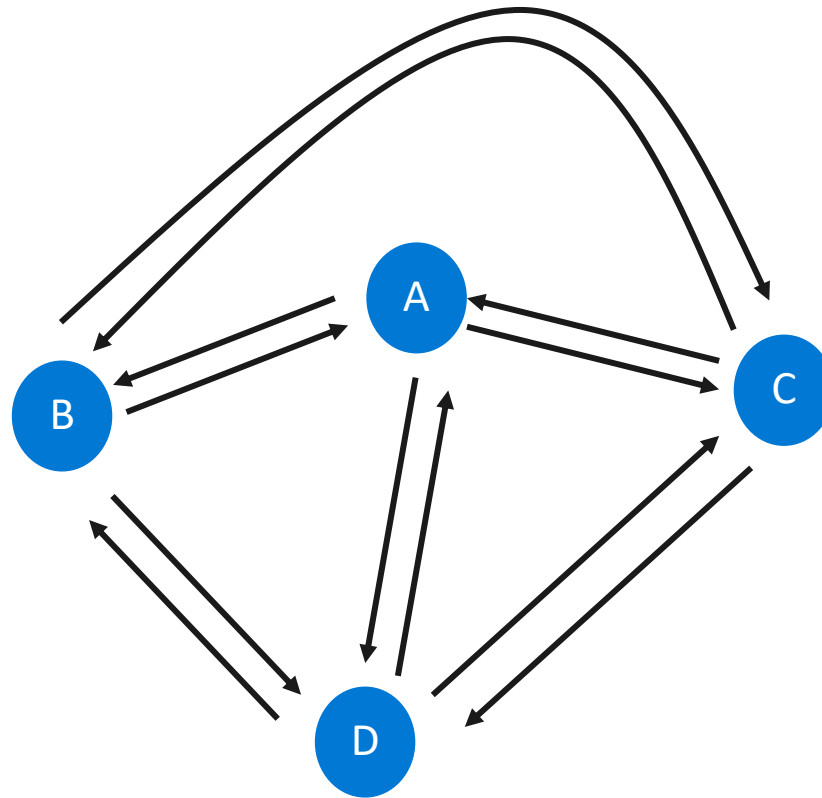
# Special Case 2: "Deep Sets"



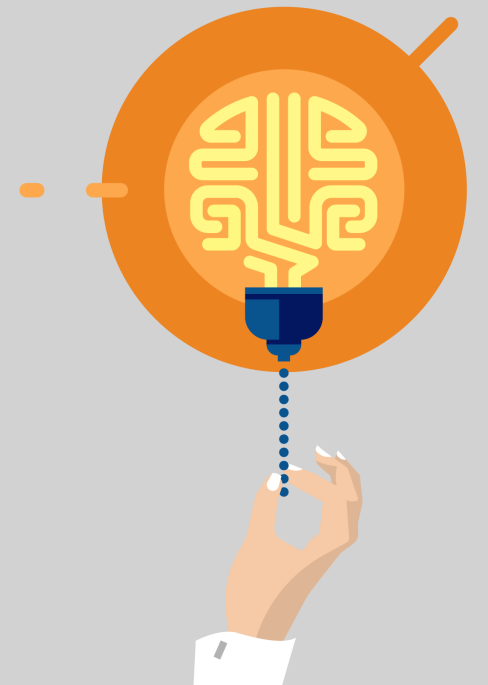
Set of Objects

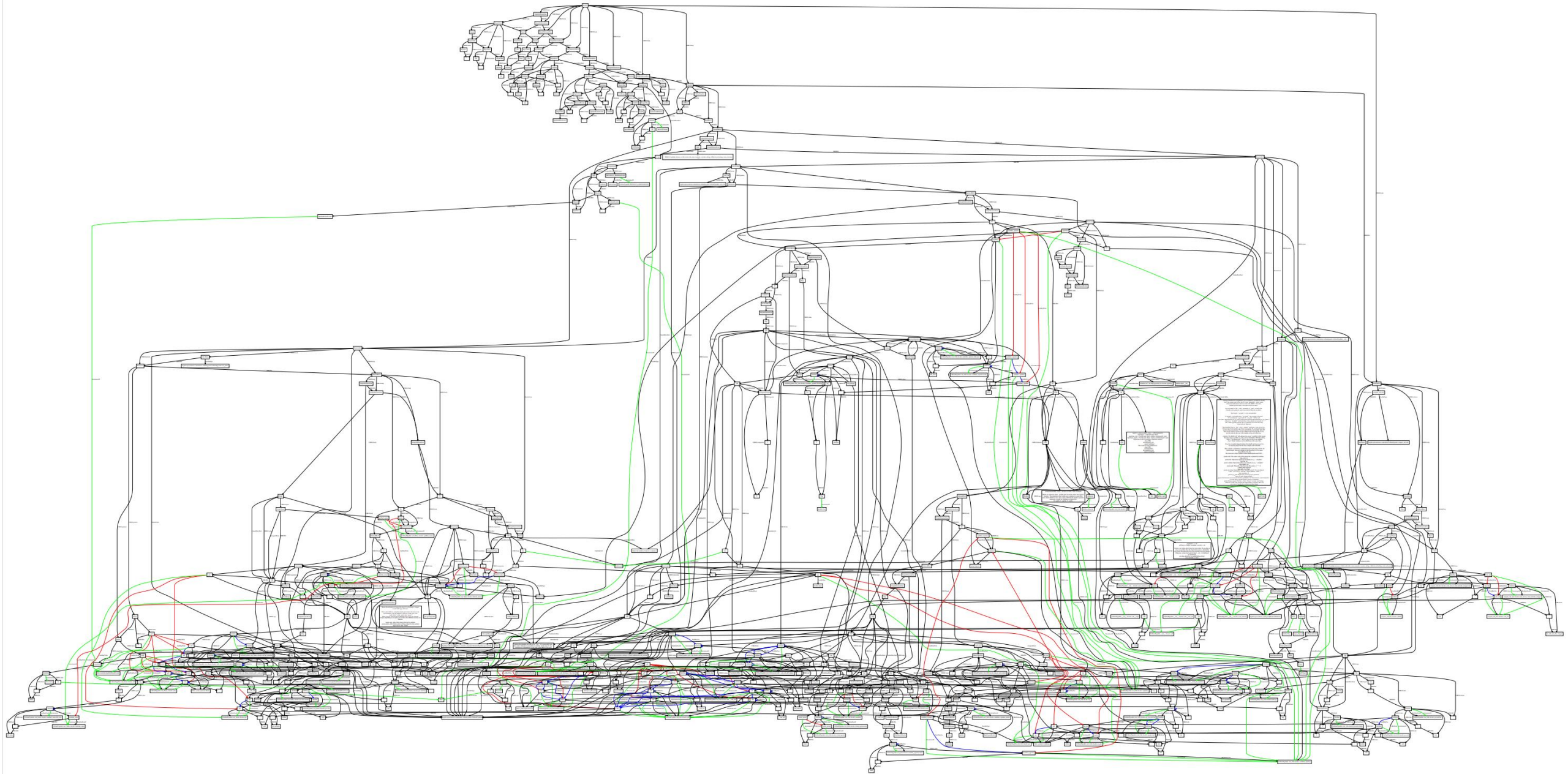
Representing a variable-sized set of objects

# Special Case 2: Self-Attention ( $\approx$ Transformers)



# GNNs in Software Engineering





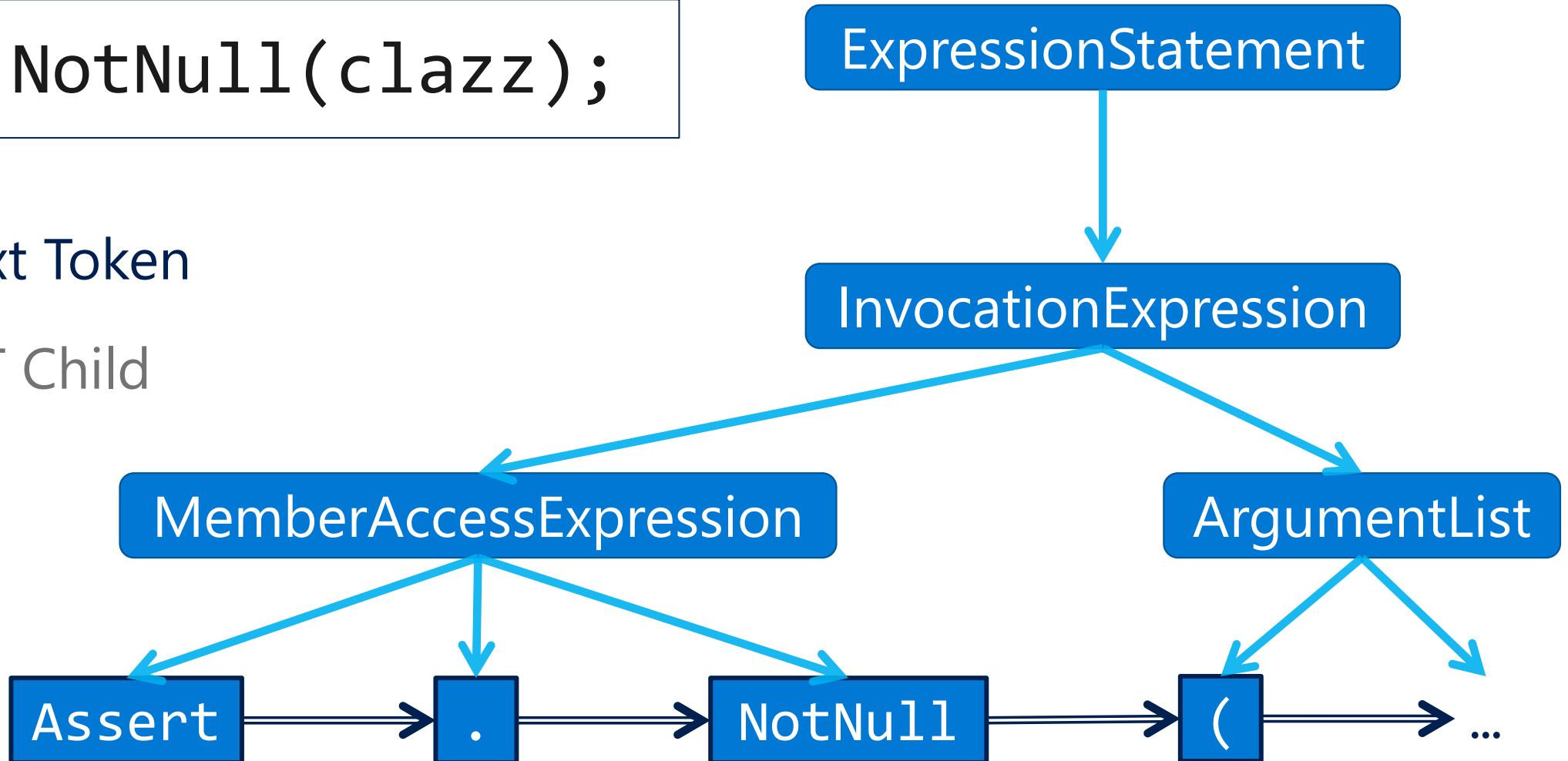
**Programs are Graphs**

# Programs as Graphs: Syntax

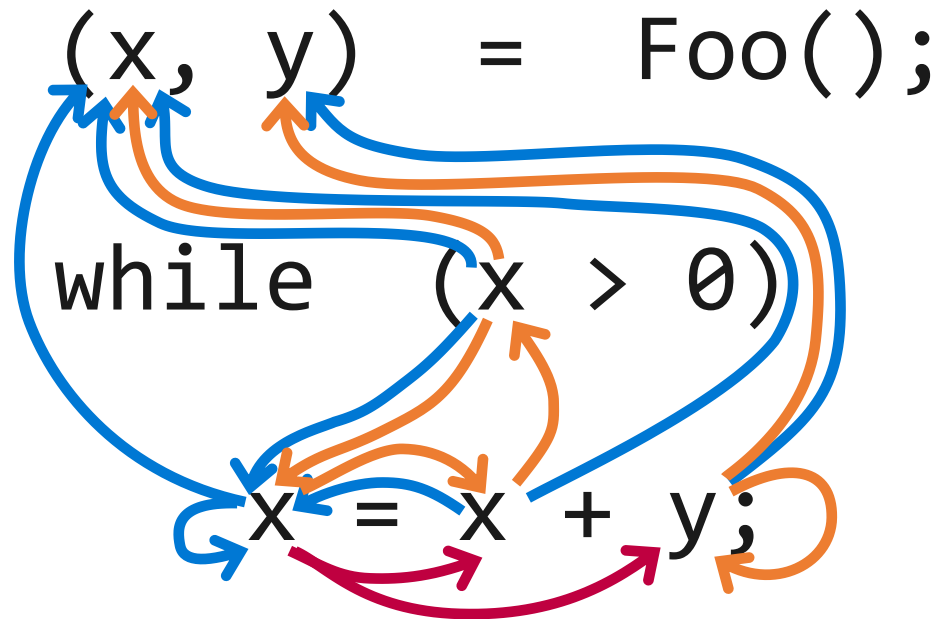
```
Assert.NotNull(clazz);
```

⇒ Next Token

→ AST Child



# Programs as Graphs: Data Flow



→ Last Write

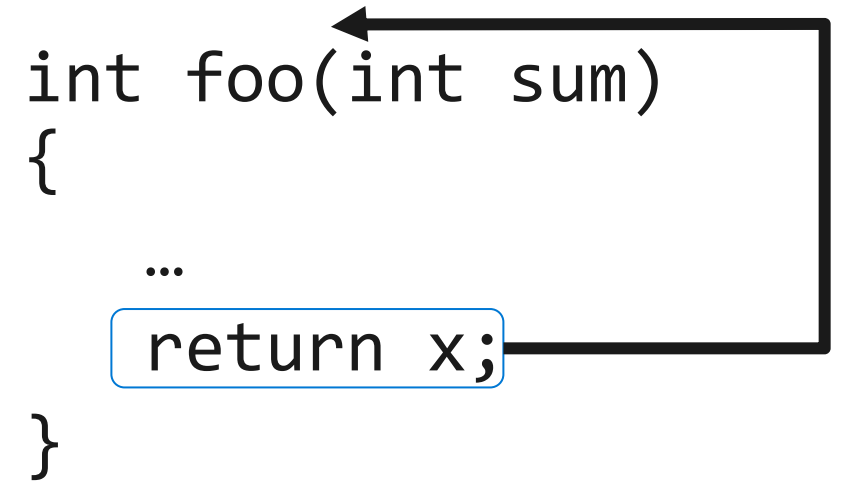
→ Last Use

→ Computed From

# Representing Program Structure as a Graph

Additional Edge Types:

- ReturnsTo



# Representing Program Structure as a Graph

Additional Edge Types:

- ReturnsTo
- FormalArgName

```
b = foo(result);
```



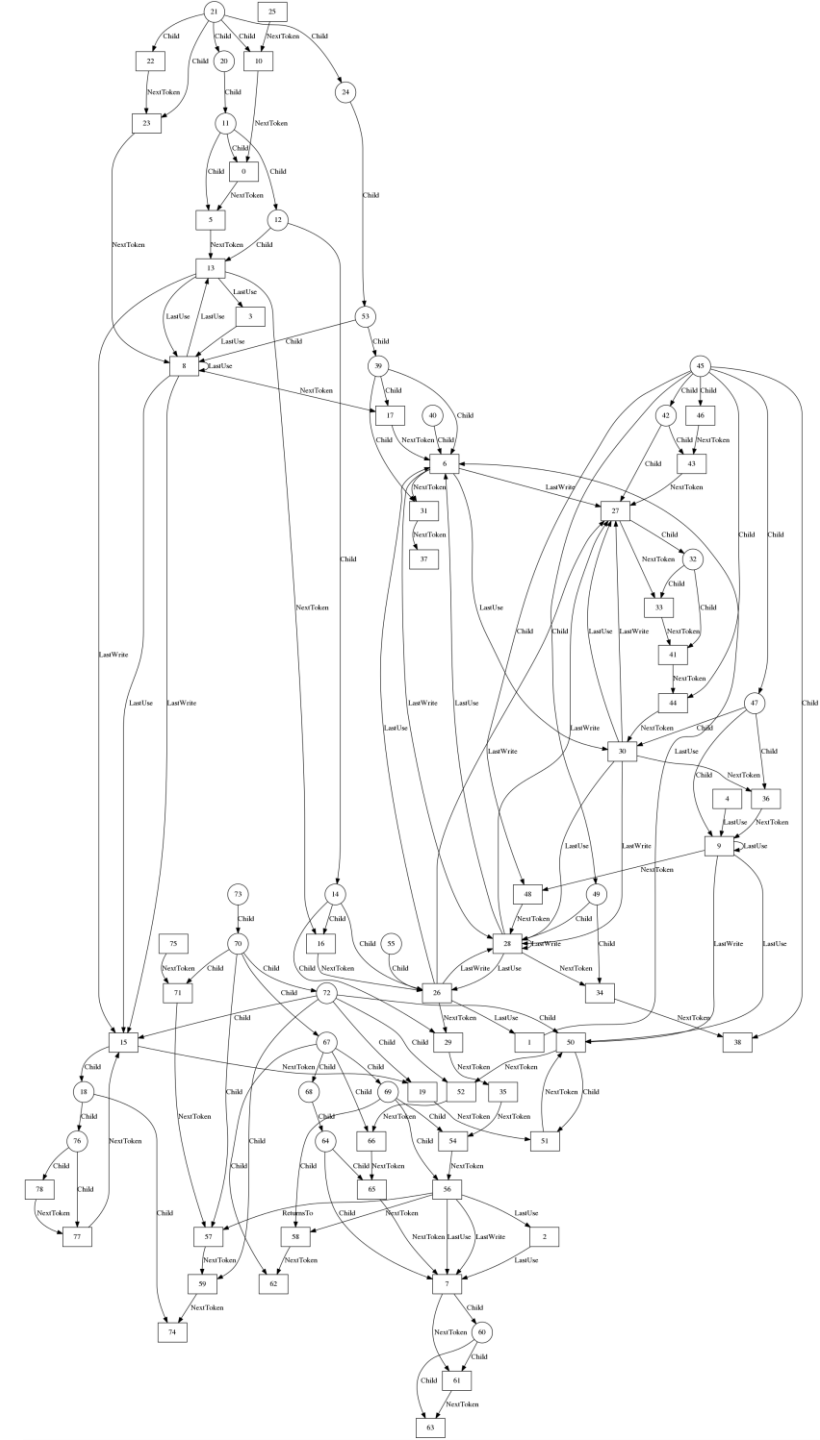
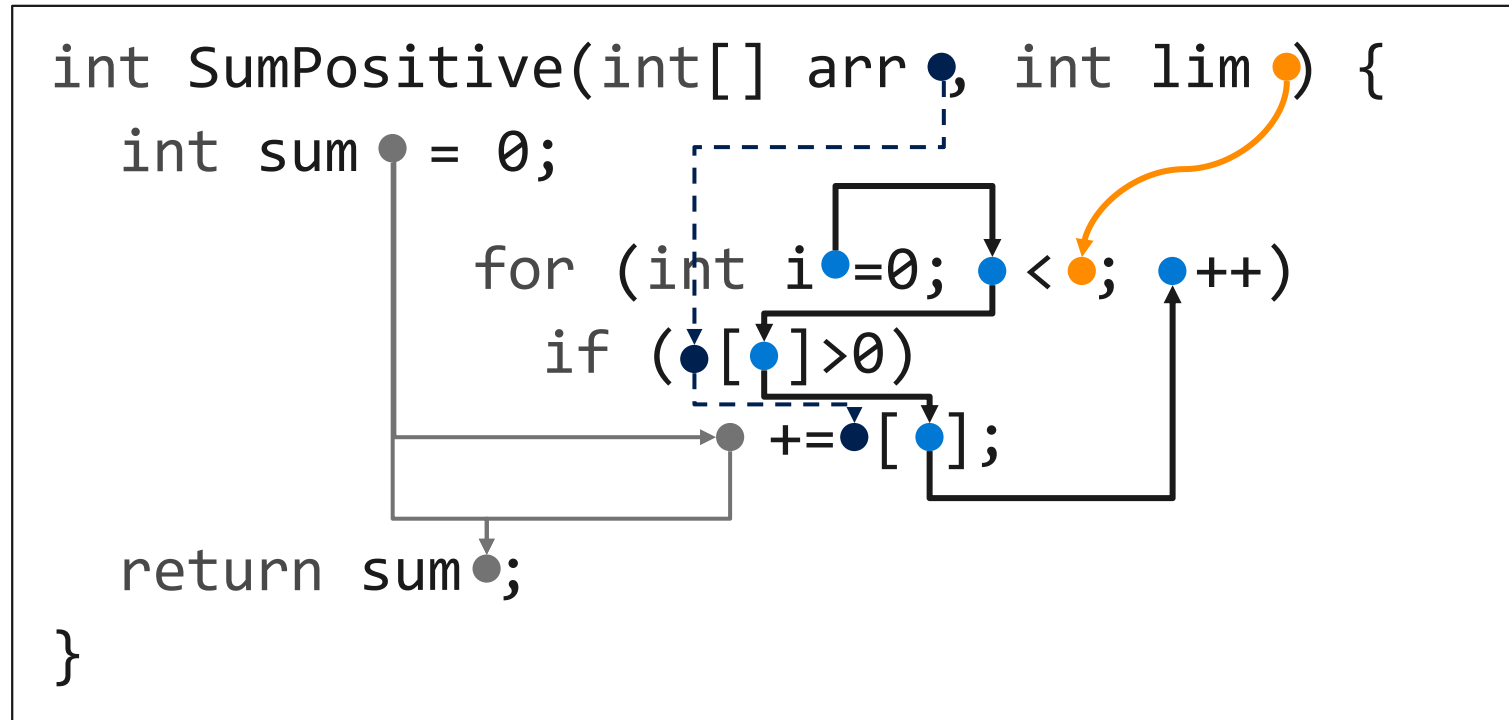
sum

```
void foo(int sum) { ... }
```

# Representing Program Structure as a Graph

Entities in Programs → Nodes

Relationships among entities → Edges



# Tasks Explored in Literature

- **VarMisuse** Allamanis *et al.* 2018, Cvitkovic *et al.* 2019, Hellendoorn *et al.* 2020
- **Method Naming** Fernandes *et al.* 2019
- **Code Generation or Repair** Brockschmidt *et al.* 2019, Yasunaga *et al.* 2020
- **Predicting Program Properties**
  - **Type Annotations in Dynamic Languages** Wei *et al.* 2020, Allamanis *et al.* 2020, Schrouff *et al.* 2019
  - **Performance Characteristics of Programs** Tomczak *et al.* 2019

# Variable Misuse Task

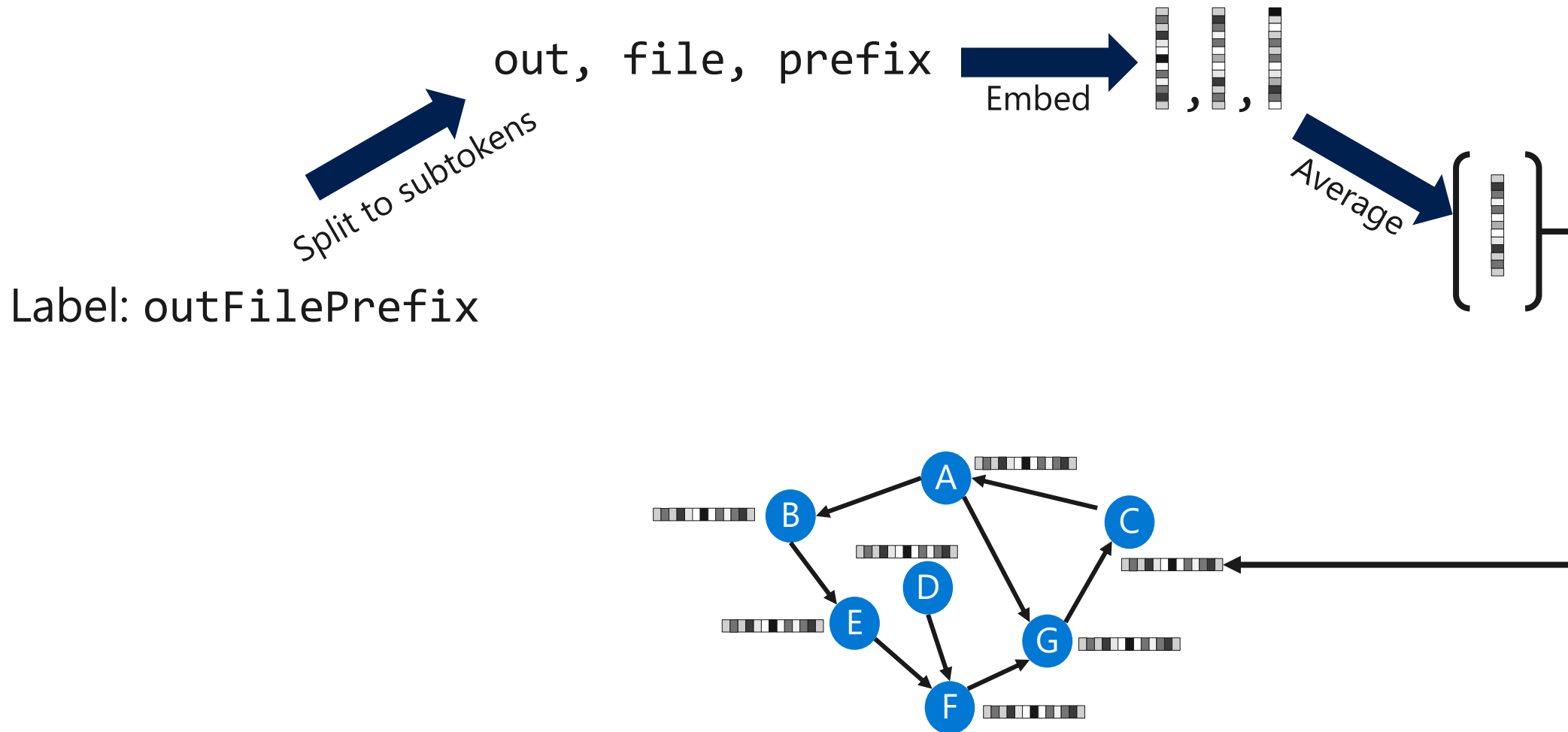
```
var clazz=classTypes["Root"].Single() as JsonCodeGenerator.ClassType;
Assert.NotNull(clazz);

var first=classTypes["RecClass"].Single() as JsonCodeGenerator.ClassType;
Assert.NotNull(clazz);

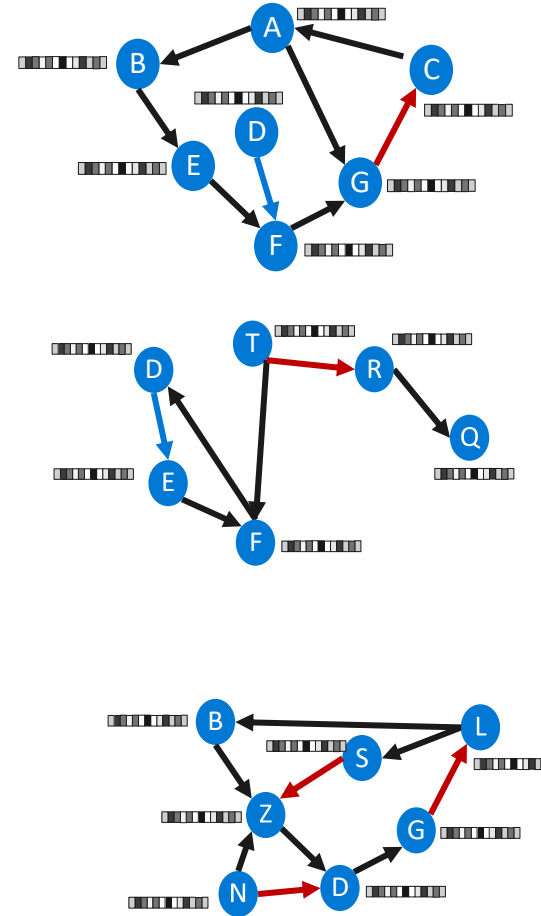
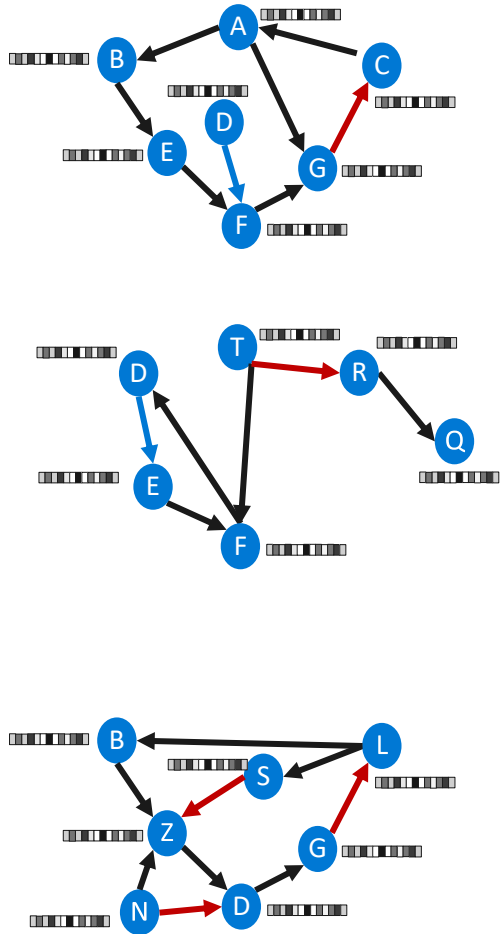
Assert.Equal("string", first.Properties["Name"].Name);
Assert.False(clazz.Properties["Name"].IsArray);
```

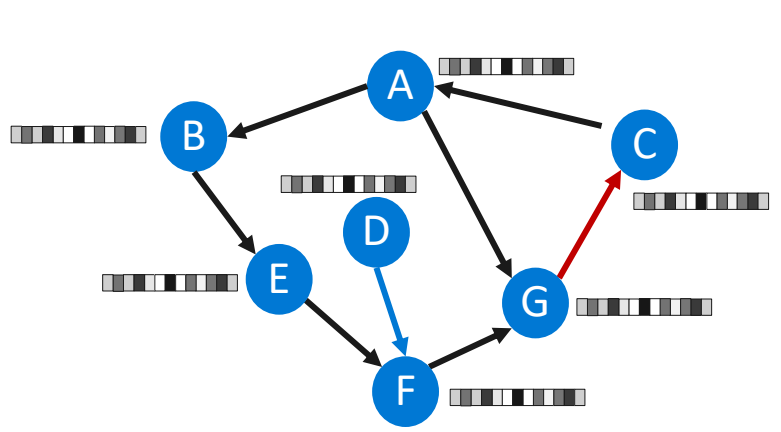


# Initial Node Representations

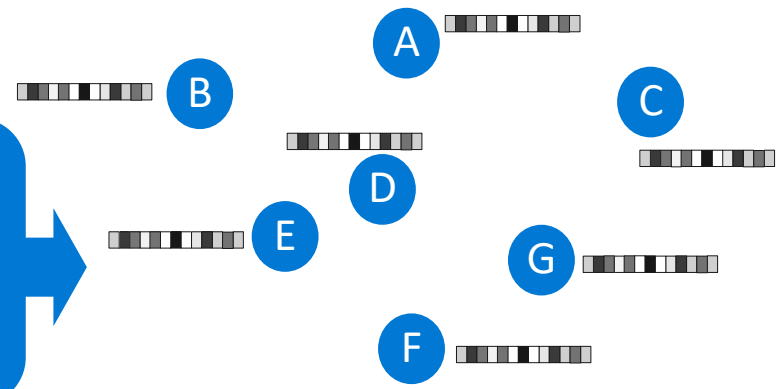


# Variable Misuse

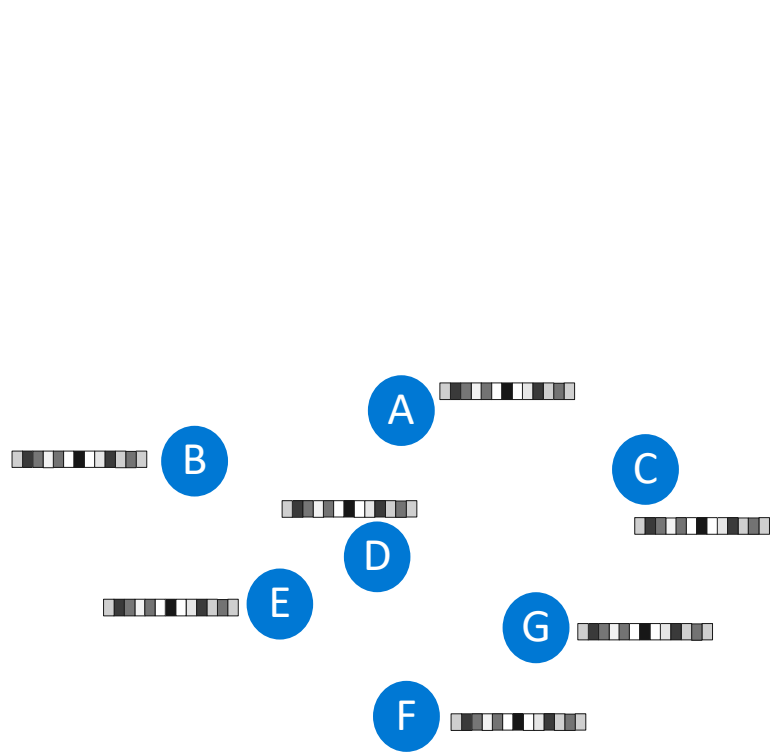




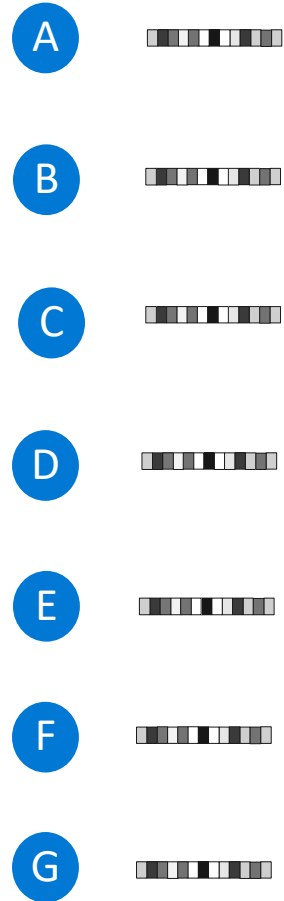
Initial Representation of each node



Output Representations of each Node



Output Representations of each Node



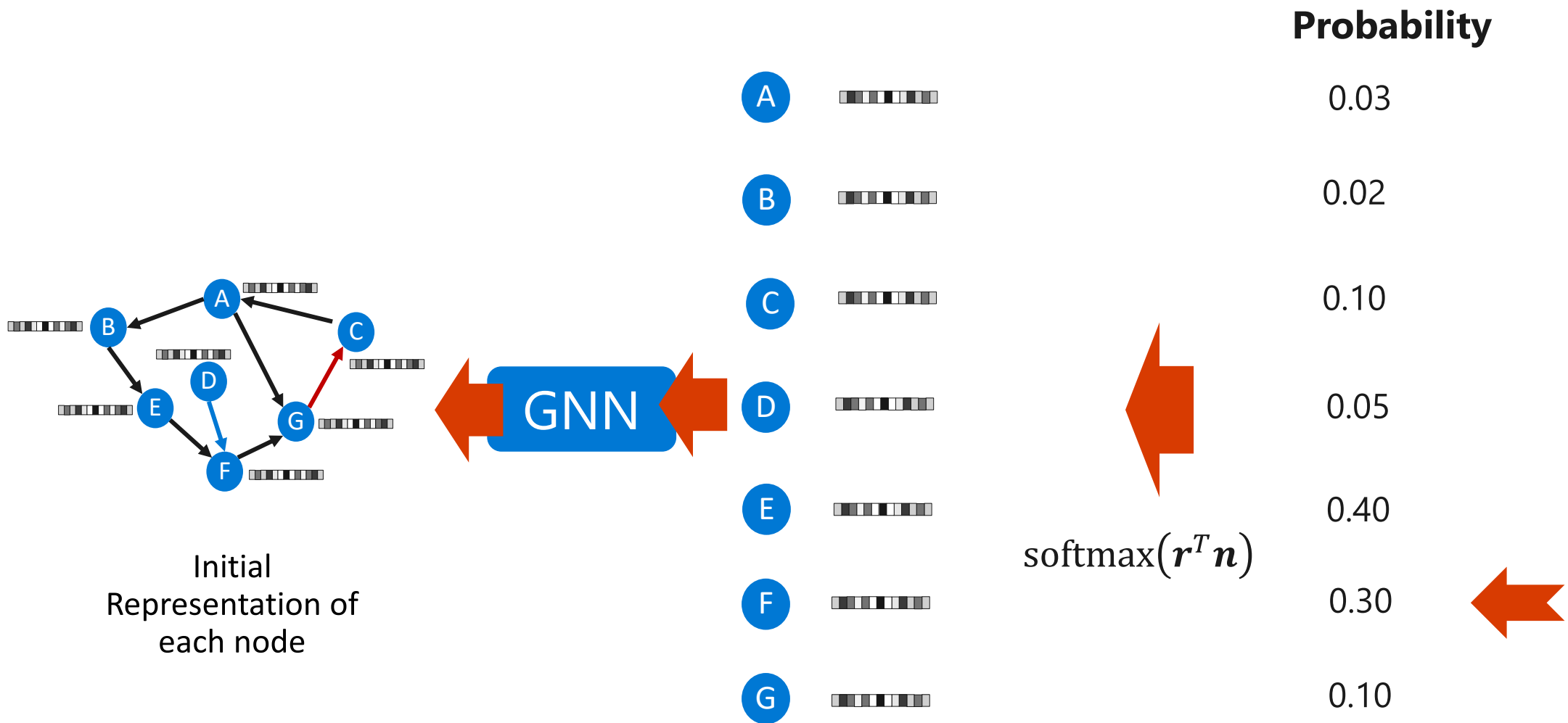
$\text{softmax}(\mathbf{r}^T \mathbf{n})$

**Probability**

- 0.03
- 0.02
- 0.10
- 0.05
- 0.40
- 0.30
- 0.10

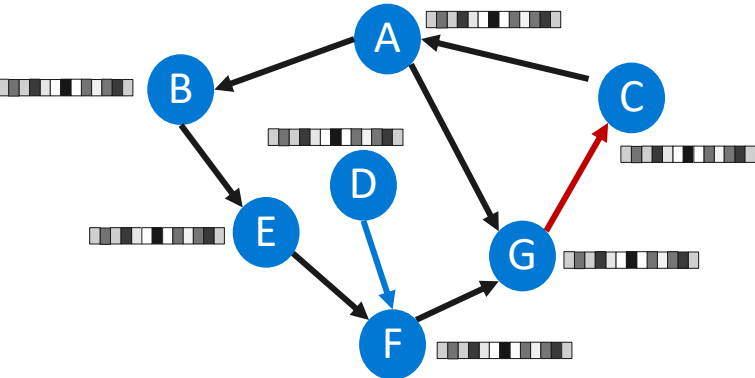


Localization objective: Pick the right node

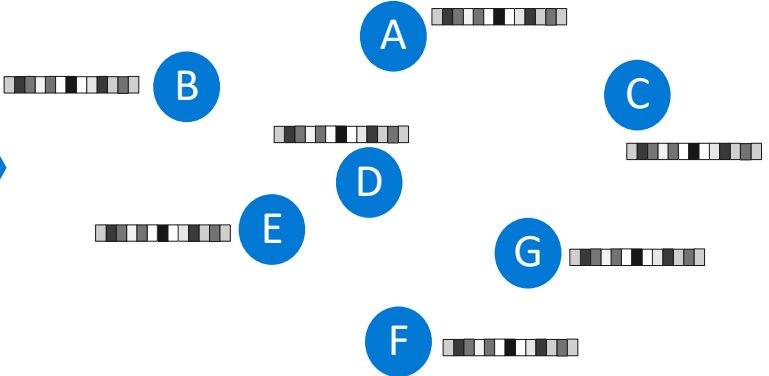
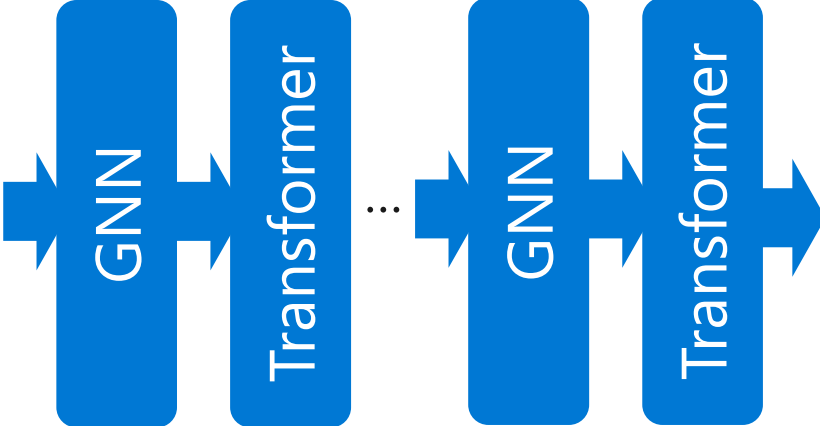


Localization objective: Pick the right node

# GNN Layers



Initial Representation of each node

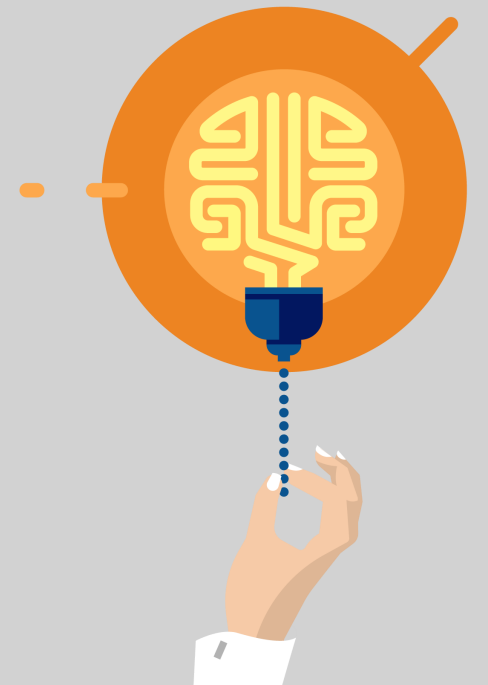


Output Representations of each Node

Model Family	Class. Accuracy		Loc & Rep Accuracy		Parameters	Training Time
	$\leq 250$	$\leq 1000$	$\leq 250$	$\leq 1000$		
RNN <sup>1</sup>	71.8%	70.6%	44.4%	42.5%	4.3M	31.3h
Transformer	75.9%	73.2%	67.7%	63.0%	3.7M	41.5h
GGNN	81.4%	79.2%	64.0%	60.9%	5.5M	241h
RNN Sandwich	<b>82.5%</b>	<b>81.9%</b>	75.8%	<b>73.8%</b>	12.6M	109h
Transformer Sandwich	81.1%	78.1%	74.5%	71.4%	10M	161h
GREAT	80.1%	76.9%	<b>76.4%</b>	73.1%	7.9M	120h

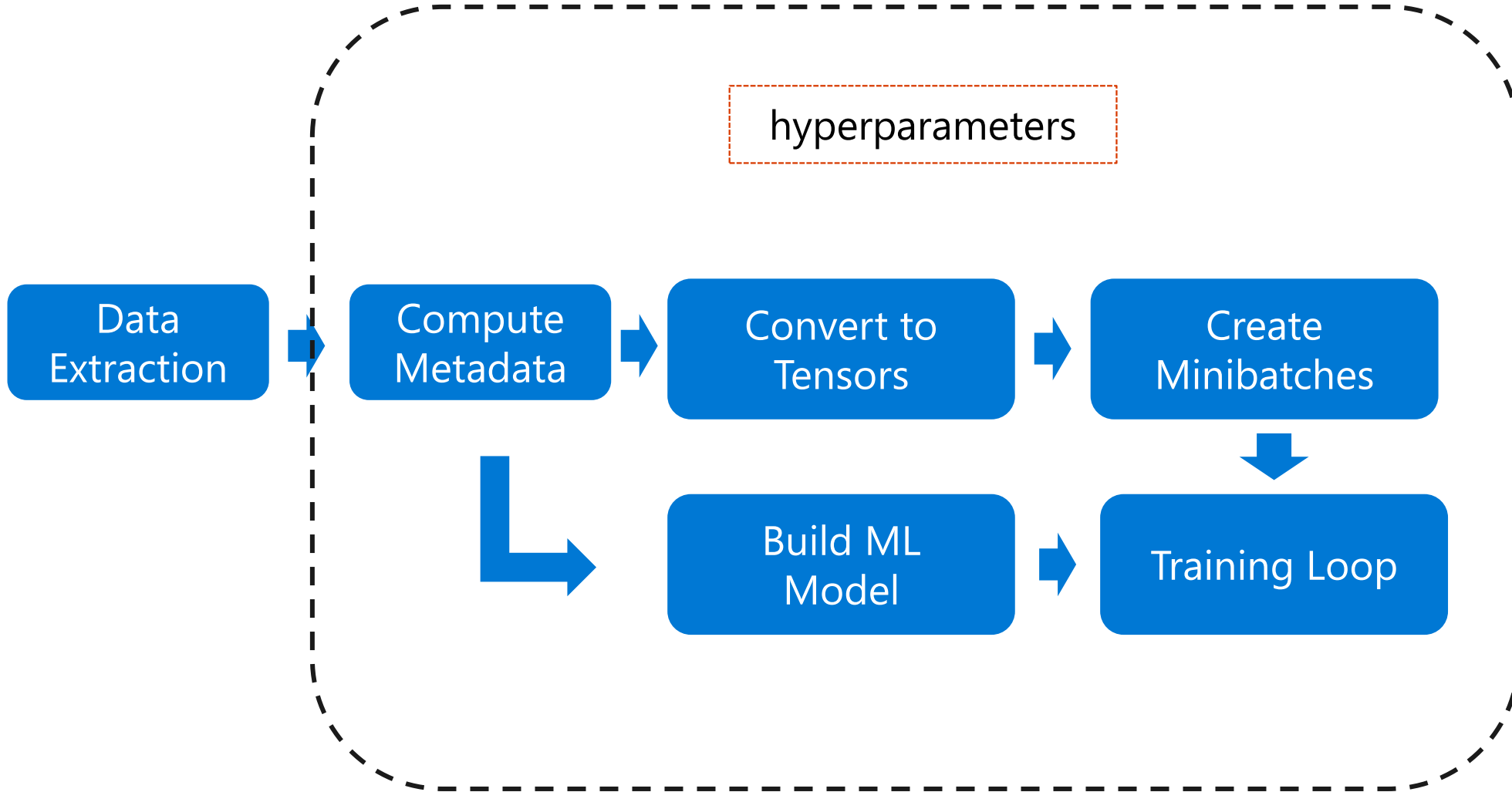
1: a stronger version of the model proposed in [Vasic et al. \(2019\)](#) (previous SOTA).

# Machine Learning in Practice





# Common Architecture of Deep Learning Code



THIS IS YOUR MACHINE LEARNING SYSTEM?

YUP! YOU POUR THE DATA INTO THIS BIG PILE OF LINEAR ALGEBRA, THEN COLLECT THE ANSWERS ON THE OTHER SIDE.

WHAT IF THE ANSWERS ARE WRONG?

JUST STIR THE PILE UNTIL THEY START LOOKING RIGHT.



## Practical(?) Tips on Debugging Machine Learning Models

### Model Capacity (*what can the model learn?*)

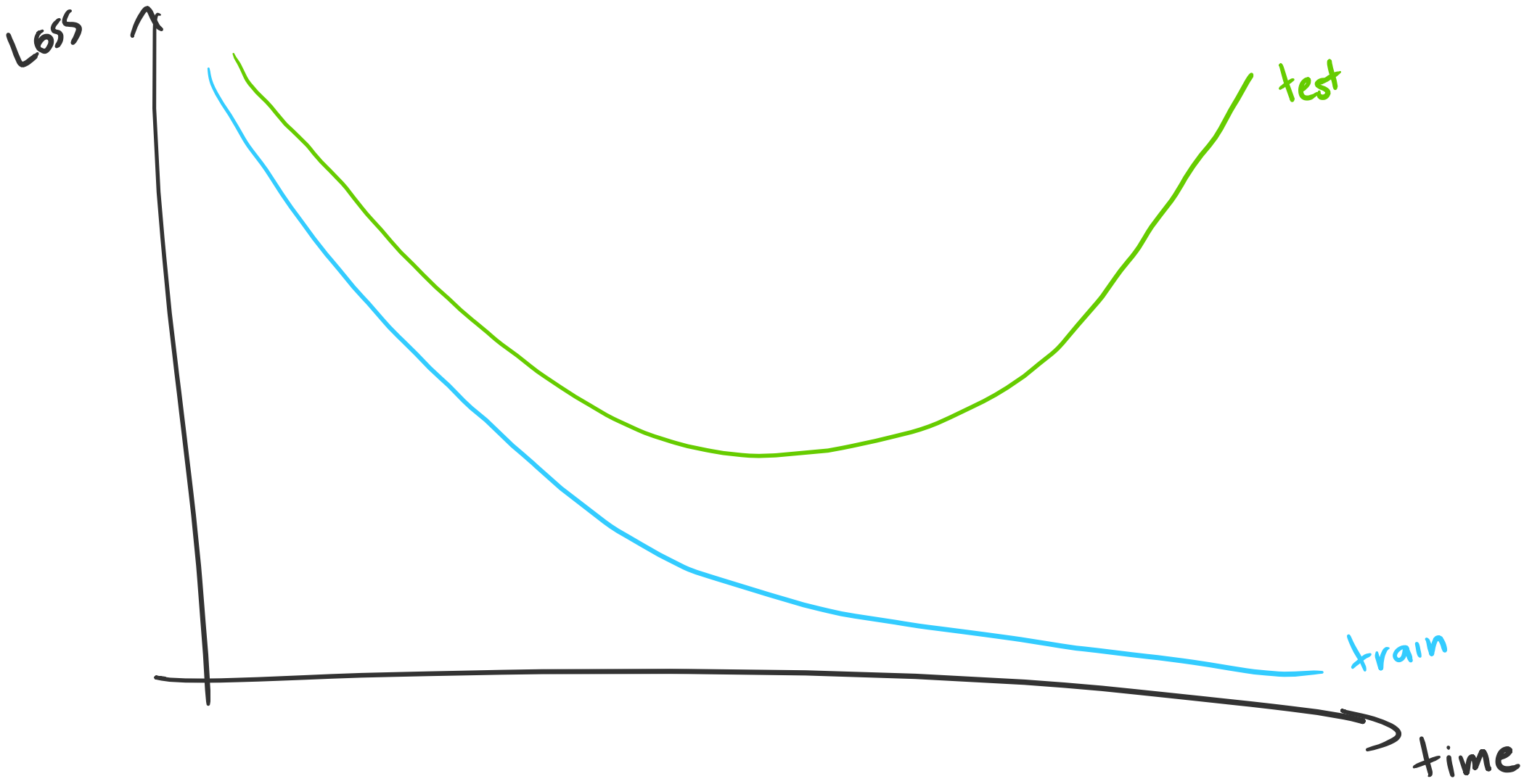
- Overtrain on a small dataset
- Synthetic data

### Optimization Issues (*can we make the model learn?*)

- Look at learning curves
- Monitor gradient update ratios
- Hand-pick parameters for synthetic data

### Other model "bugs" (*is the model doing what I want it to do?*)

- Generate samples from your model (if you can)
- Visualize learned representations (*e.g.* embeddings, nearest neighbors)
- Error analysis (examples where the model is failing, most "confident" errors)
- Simplify the problem/model
- Increase capacity, sweep hyperparameters (*e.g.* increase size of **h** in LSTM)

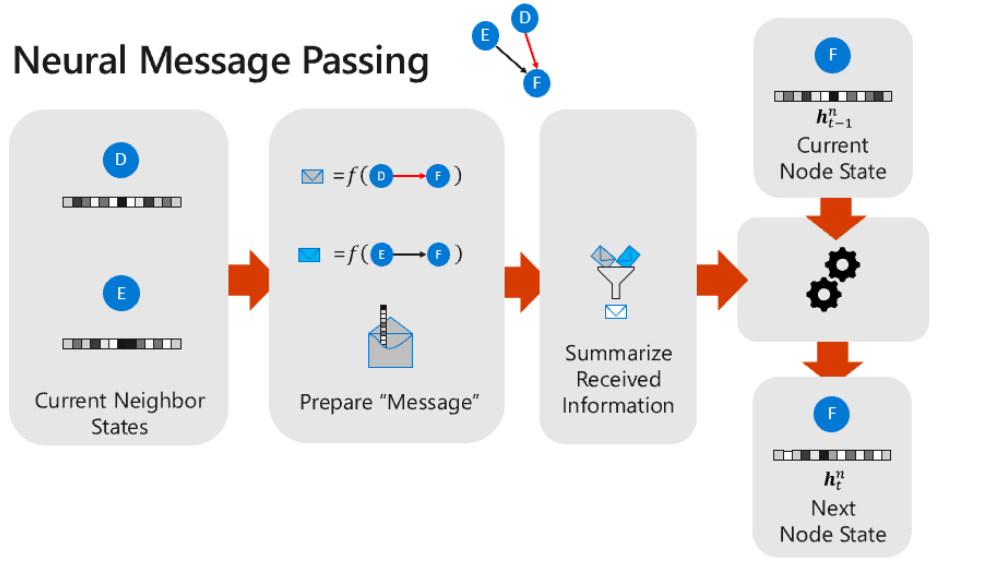


Learning Curve

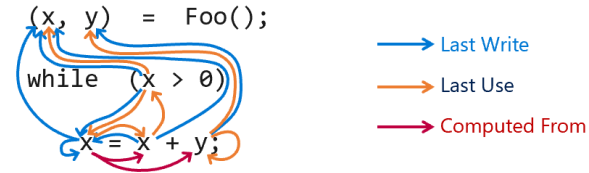


# Graph Neural Networks in SE Research

## Neural Message Passing



## Programs as Graphs: Data Flow



## Variable Misuse Task

```
var clazz=classTypes["Root"].Single() as JsonCodeGenerator.ClassType;  
Assert.NotNull(clazz);  
var first=classTypes["RecClass"].Single() as JsonCodeGenerator.ClassType;  
Assert.NotNull(clazz);  
Assert.Equal("string", first.Properties["Name"].Name);  
Assert.False(clazz.Properties["Name"].IsArray);
```

Allamanis et al. 2018, Cvitkovic et al. 2019, Hellendoorn et al. 2020



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